

## NONLINEAR MEMS MECHANISM FOR ENERGY HARVESTING FROM MECHANICAL VIBRATIONS

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### Abstract

Energy harvesting materials, renewable power sources, scavenging techniques and autonomous sensor nodes that save energy from the environment, have emerged as a prominent research area and in continuous development. The interest to save energy from the environment is highly felt in small and also integrated scale: self powered integrated systems, autonomous MEMS transducers, batteryless sensor node, self-powered sensors, smart systems [1], represent a set of devices that adopt the harvested energy to sustain or to supply an electronic device. Different kinds of energy can be harvested from renewable natural sources, such as: sunlight power, thermal gradients, wind, rain, tides, acoustic, and mechanical vibrations. In particular the last one represents an available source and presents a significant energy amount. It is present in nature as earth's vibration, seismic vibrations, naturally noise source and different energy converters can be adopted such as: piezoelectric, electromagnetic, and electrostatic transducers. A classical approach is represented by a mechanically resonant device that is, suitably, matched to the single tone vibration of the source. However, in the vast majority of cases the ambient mechanical vibrations come in a vast variety of forms and having the energy distributed over a wide spectrum of frequencies, typically distributed in a bandwidth of few thousands of Hz. Several ways for optimization have been explored, concerning the increment of the converted and extracted energies, and the transduction mechanisms [2]. A different approach is presented here: it is based on the exploitation of the properties of "nonresonant" MEMS oscillators characterized by a nonlinear dynamic response. For these oscillators, it is not possible to define a transfer function, and thus a properly defined resonant frequency, even if the power spectral density can show one or more well defined peaks. Furthermore a wider spectrum is predicted for the nonlinear system with respect to the linear oscillator. The nonlinear behaviour has been previously demonstrated on macro cantilever prototypes [3, 4]. The figure 1 shows the bistable mechanism applied in a U-shaped MEMS device and the dynamic model assumed as a nonlinear pendulum governed by a double well nonlinearity [3, 4]:

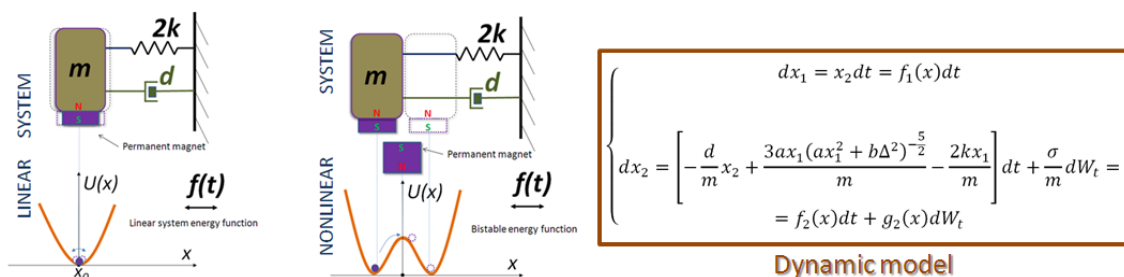


Figure1: Bistable MEMS mechanism, on the left: high distance between the two magnets implies a linear behaviour and the parabolic function describes the energy. Furthermore two equilibrium states  $x_1$  and  $x_2$  will appear when the mass spring damper system is subjected to the effect of the neighbor external magnet;  $x_0$  represents an unstable condition (on the right). The term  $2k$  represents the contribution of the two parallel springs,  $d$  is the damper and  $m$  the mass at the tip of the cantilever. In red, the dynamic model is presented.

Where  $\Delta$  is the distance between the two magnets (the first deposited onto the cantilever surface and the second, in the external part of the system, and maintained fixed);  $a$  and  $b$  represent constants correlated to the physical parameters of the systems. In presence of a stochastic source,  $f(t)$  assumes non periodic oscillations, so the dynamic can be described through a stochastic differential equation. The system of equations is composed by two 1<sup>st</sup> order Itô's equations with two drift terms,  $f_1(x)$  and  $f_2(x)$ : the first represents the velocity of the cantilever tip, the latter is function of the damping ( $d$ ), the elastic constant ( $k$ ) and an additive nonlinear term. Only one diffusion term is included in the system  $g_2(x)$ , that is function of the vibrations amplitude ( $\sigma$ , standard deviation of the source) and the mass ( $m$ ) of the nonlinear oscillator;  $x_l$  is the displacement of the cantilever tip, and  $t$  is the time. The previously model has been simulated by using MATLAB<sup>®</sup> SDE (Stochastic Differential Equation) Toolbox. The Euler-Maruyama method has been used with vibration source (gaussian white noise) having a standard deviation ( $\sigma$ ) of 20  $\mu\text{N}$ . The figure 2a shows the simulation result of an U-shaped cantilever device having an elastic constant of 12  $\text{kg/s}^2$  and based on two parallel cantilever beams having a length of 2500  $\mu\text{m}$  and width of 700  $\mu\text{m}$ , connected at their free extremity by a 'linking arm' (3400  $\mu\text{m}$  x 700  $\mu\text{m}$ , the thickness is 15  $\mu\text{m}$ ). A resonance spike has been detected at  $\Delta=0.933$  mm. The integrated system has been also realized by using the BESOL technology [5] (figure2d). The principle has been experimentally validated by using an external permanent magnet stack and a translator system, in order to modulate the distance between the two magnets, a shaker has been used to stimulate the structure, an active Wheatstone bridge has been used as conditioning circuit and a LabVIEW<sup>™</sup> routine has been performed to filter and to drive the shaker using a GPIB communication. A resonance condition has been experimentally verified that represents the maximum value of the beam displacement and a bistable condition with a low energy barrier. Coherence as respect the simulation results has been detected ( $\Delta=0.94$  mm). Figure 2c shows the output signal of the bridge when a distance of 0.94 mm between the two magnets occurs, while figure 2b shows the output spectrum evaluated through the measure campaign: a wider spectrum compared to the linear case appears for the nonlinear system, so more energy can be saved adopting a bistable dynamic. The proposed mechanism validated for a MEMS device, evinces an improvement of the performance with respect to a linear oscillator. The obtained results confirm the nonlinear principle applied to a MEMS device, moreover they represent a major advance with respect to the state of the art in the integrated energy harvesting area; in fact the device that has been designed, realized and validated can be highly efficient for scavenging energy from a large range of vibration sources having different nature and therefore different spectral content. As a future trend a PZT material and magnetic stack deposition will be performed.

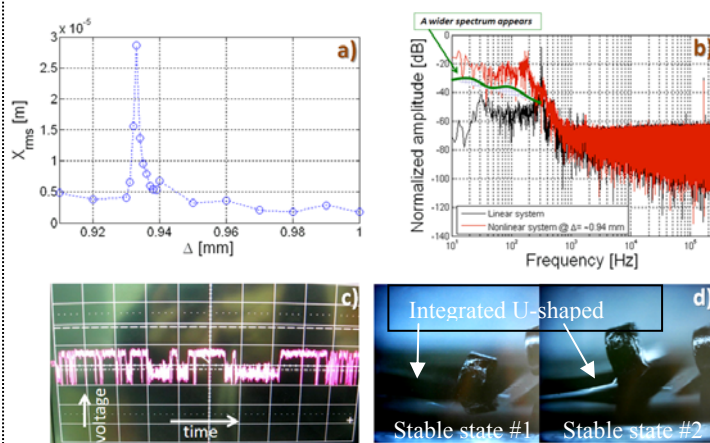


Figure2: a) Simulation result: displacement of the U-shaped device (AC component), excited by gaussian vibrations having standard deviation ( $\sigma$ ) of 20  $\mu\text{N}$ . Experimental results: b) Output spectrum in the linear case (black) and in the nonlinear case (red). A wide spectrum appears in presence of a bistable energy function, c) scope picture of the Wheatstone bridge output at  $\Delta=0.94$  mm and  $\sigma=20$   $\mu\text{N}$ . d) Microscope picture of the U-shaped device realized with the permanent magnet deposited at the tip; in front, the tunable magnetic stack: on the left the first stable state; on the right, second stable state.

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