



Article

Modeling Aerial Transmission of Pathogens (Including the SARS-CoV-2 Virus) through Aerosol Emissions from E-Cigarettes

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Abstract: We examine the plausibility of aerial transmission of pathogens (including the SARS-CoV-2 virus) through respiratory droplets that might be carried by exhaled e-cigarette aerosol (ECA). Given the lack of empiric evidence on this phenomenon, we consider available evidence on cigarette smoking and respiratory droplet emission from mouth breathing through a mouthpiece as convenient proxies to infer the capacity of vaping to transport pathogens in respiratory droplets. Since both exhaled droplets and ECA droplets are within the Stokes regime, the ECA flow acts effectively as a visual tracer of the expiratory flow. To infer quantitatively the direct exposure distance, we consider a model that approximates exhaled ECA flow as an axially symmetric intermittent steady starting jet evolving into an unstable puff, an evolution that we corroborate by comparison with photographs and videos of actual vapers. On the grounds of all this theoretical modeling, we estimate for low-intensity vaping (practiced by 80–90% of vapers) the emission of 6–210 (median 39.9, median deviation 67.3) respiratory submicron droplets per puff and a horizontal distance spread of 1–2 m, with intense vaping possibly emitting up to 1000 droplets per puff in the submicron range with a distance spread over 2 m. The optical visibility of the ECA flow has important safety implications, as bystanders become instinctively aware of the scope and distance of possible direct contagion through the vaping jet.

Keywords: electronic cigarettes; droplet dynamics; bioaerosols; turbulent jets; COVID-19

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1. Introduction

The evolution of bioaerosols spreading disease contagion through respiratory droplets has been widely studied, as can be appreciated in reviews on generic pathogens by Galton et al. [1] and Zhang et al. [2], the influenza and SARS viruses [3,4] and in spread risk modeling [5] (see the chapter on bioaerosols and cited references therein in [6]). As expected, the current COVID-19 pandemic has motivated the study of direct and indirect aerial transmission of the SARS-CoV-2 virus through various expiratory activities.

There is currently a broad consensus, endorsed by the WHO [7] and the CDC [8], that contagion of the SARS-CoV-2 virus occurs either by close range exposure to relatively large droplets emitted by infectious individuals or through indirect exposure to smaller submicron droplets denoted by the term “aerosols” (see, e.g., [9–12]), although the scope and relevance of each contagion route depend on local factors (volume, occupancy and ventilation regimes of inner spaces) [13–18]. The 5 µm cut-off separating larger droplets and “aerosols” is merely a convention that artificially simplifies droplet dynamics that vary

along a continuous spectrum of diameters into two mutually exclusive modalities; thus, we avoid as much as possible the binary “droplets” vs. “aerosols” terminology.

The purpose of the present paper is to fill an important gap in the above-mentioned body of literature on pathogen (including SARS-CoV-2) spread through respiratory droplets, namely to examine the plausibility, scope and risks of this transmission taking place through a different expiratory route: exhaled e-cigarette aerosol (ECA). While there is no factual evidence or proper elaborate research (a search of the literature revealed three opinion pieces [19–21] that offer a very limited argumentation) on pathogen transmission through this vehicle, we hypothesize that it is entirely plausible that it occurs, simply because vaping (usage of e-cigarettes) is an expiratory activity (as well as smoking). To fulfill this task, we need to develop a comprehensive and interdisciplinary theoretical modeling of this phenomenon, proceeding along the following methodological steps:

1. The wide variety of vaping styles and puffing protocols bears influence on respiratory parameters. We follow a practical and convenient simplification of this intensity spectrum by considering two principal modes: a low-intensity style (“mouth to lung”) style and a high-intensity one (“direct to lung”)
2. Available evidence on the physical and physicochemical properties of ECA show that its particulate phase (submicron liquid droplets) evolves within the Stokes regime, in which viscous forces dominate over inertial forces, so that particle Reynold numbers are negligible ($Re_p \ll 1$). As a consequence, the particles trace the fluid flow (basically exhaled air) roughly as tracer gases or molecular contaminants.
3. To infer the respiratory dynamical parameters that can be associated with vaping, we need to estimate the volume of exhaled ECA aerosol per puff (vaping tidal volume) and its exhalation velocity. We use for this purpose available data on a very useful proxy: cigarette smoking. Since vaping involves suction through a mouthpiece, we also need to look at the effects of these instruments on respiratory parameters.
4. Given the outcomes of the previous step, we estimate a range of exhalation velocities that can associated with vaping. Comparing this velocity range with exhalation velocity data for various respiratory activities, we infer that mouth breathing through a mouthpiece provides an appropriate proxy for estimating the size and numbers of respiratory droplets that should be transported by exhaled ECA.
5. Considering available observational and experimental data on droplet emission from mouth breathing, we infer that ECA flow should be overwhelmingly carrying submicron desiccated droplets of the type known as “aerosols”. Just as ECA droplets, these “aerosols” lie in the Stokes regime, so that the exhaled ECA flow provides an accurate visual tracing to infer how far they can be transported to produce direct exposure to bystanders located in the direction of this flow.

Given these estimations and inferences, we model the exhaled ECA flow in an indoor space with natural ventilation as a turbulent isothermal starting jet evolving into an unstable puff, evaluating the maximal distance for direct exposure to respiratory droplets potentially carried by vaping exhalations. This theoretical jet/puff model seems to provide a reasonable approximation to real life vaping jet/puff systems seen in photographs and videos of actual vapers vaping (see Section 5.3 and the Supplementary Material SM(3)). We do not consider in this paper indirect exposure to desiccated respiratory droplets (“aerosols”) that might remain extended times in the environment after this jet evolves into an unstable puff and disperses, as the dynamics of these particles depends on indoor air currents and not on the vaping jet.

The relevance of the present paper follows from the fact that the current COVID-19 pandemic has forced millions of vapers, smokers and non-users surrounding them into sharing indoor spaces under various degrees of home confinement. Objective research on COVID-19 transmission through exhaled ECA can serve to guide evidence-based public policies to address public health concerns and risk management and minimization to address this phenomenon. Given the relevance of safety assessment in the context of the COVID-19 pandemic, we elaborated two articles related to (but fully independent from) the

present article: one is a full risk analysis of vaping emissions in shared indoor spaces [22], while the other is a short article [23] discussing their public health and public policy implications, as well as reviewing available evidence on the relations between COVID-19 and smoking and vaping.

It is necessary to issue the following important disclaimer: The present article is concerned only with the plausibility, scope and risks of pathogen (including SARS-CoV-2) transmission through exhaled ECA, not with vaping as a possible risk factor for becoming infected by the virus or for any evolution or stage of adverse health outcomes associated with COVID-19 (these issues are examined in [23]). In addition, we are not concerned with possible health hazards by users' exposure to inhaled ECA or bystanders to exhaled ECA derived from the usage of e-cigarettes as substitute of tobacco smoking. Readers are advised to consult the available literature on these subjects (see extensive reviews [24–28]).

Another important disclaimer: this paper does not address potential COVID-19 contagion through respiratory droplets carried by environmental tobacco smoke, although smoking can serve as a useful proxy for understanding the respiratory and dynamical parameters of low-intensity ('mouth to lung') puffing style practiced by 80–90% of vapers. However, most of the results we obtain are applicable to "mainstream" smoke exhalations emitted by smokers, not to sidestream emissions from the burning/smouldering tip of cigarettes, cigars and pipes that make the bulk of environmental tobacco smoke.

In what follows, we provide a quick section by section summary of the paper following the methodological structure outlined above. Background material is presented Section 2: vaping styles and demographics (Section 2.1); a brief review of physical and physicochemical properties of inhaled and exhaled ECA (Section 2.2); and exhaled ECA as a tracer of expiratory fluid flow (Section 2.3). Section 3 (Methods) provides the material needed to infer respiratory mechanics and possible respiratory droplet emission for vaping: the effects of suction (Section 3.1) and mouthpieces (Section 3.2), and then evidence on droplet emission from mouth breathing that should provide an appropriate proxy for vaping (Section 3.3). In Section 4, we present a model of a turbulent starting jet with finite injection evolving into an unstable puff to infer the horizontal distance that respiratory droplets potentially carried exhaled ECA flow should be transported. The results obtained from these sections are summarized in Section 5. Droplet emission (Section 5.1): Low-intensity vaping should exhale 700–900 cm³ per puff, carrying 6–200 droplets (median 39.9, median deviation 67.3), overwhelmingly in the submicron range, while high-intensity vaping should exhale a tidal volume of 1000–3000 cm³ per puff carrying possibly several hundreds and up to over 1000 droplets also in the submicron range. The predictions of the jet/puff hydrodynamical model presented in Section 4 yield (Section 5.2) a horizontal distance spread between 0.5 and 2 m (low-intensity vaping) and over 2 m (high-intensity vaping) in the direction of the exhaled jet. In Section 5.3, we validate the jet/puff model by comparison with photographs and videos of actual vapers. We conclude the paper by presenting in Section 6 its limitations, together with a final thorough discussion.

2. Background

2.1. Vaping Styles and Demographics

2.1.1. Puffing Topography

Vaping is characterized by a wide range of distinct and individualized usage patterns loosely described by the parameters of puffing topography: puff and inter puff duration, puff volume and flow (see [29–32]). This style diversity complicates the study and evaluation of e-cigarette aerosol (ECA) emissions, more so given the need to upgrade standardization of vaping protocols, especially for the appropriate configuration of vaping machines used for research and regulation.

To simplify the description of vaping style, we consider two vaping topographies, MTL and DTL, described as follows

- Low-intensity "Mouth-To-Lung" (MTL). It consists of three stages: (1) "puffing", where ECA is sucked orally while breathing through the nose; (2) the puffed ECA is

withdrawn from the mouth and held in the oropharyngeal cavity without significant exhalation; and (3) inhalation into the lungs of the ECA bolus by tidal volume of air from mouth and nose inspiration. It is a low-intensity regime involving mostly low-powered devices (mostly starting kits, closed systems and recent “pods”) roughly similar to the topography of cigarette smoking.

- High-intensity “Direct-To-Lung” (DTL). Step 1 is the same as in MTL, but it bypasses Step 2. The ECA bolus diluted in tidal volume is inhaled directly into the lung without mouth retention. It is mostly a high-intensity regime associated with advanced-tank systems.

The topography parameters characterizing these styles are listed in Table 1. It is important to remark that these parameters change when vaping ad libitum in natural environments instead of doing so in a laboratory setting. This was reported by Spindle et al. [31]: for example, average puff duration was about 20% longer ad libitum, 5 s vs. 4 s in a laboratory setting.

A third puffing topography not included in Table 1 is “Mouth Puffing”: it shares Step 1 of MTL but without Step 3, with the ECA bolus diluted in tidal volume air being exhaled without lung inhalation. It is a low-intensity regime but involving higher exhaled aerosol density, since less than 5% of aerosol mass is deposited in the mouth (see [33]). Very few vapers and cigarette smokers use this style, but most smokers of prime cigars and tobacco pipes do.

Table 1. Parameters of vaping topography for vaping styles. Puff topography parameters: m_b , V_b , Φ_b are, respectively, mass (mg) (aerosol yield), volume (mL), flow (mL/s) per puff of ECA bolus (aerosol yield). Notice that tidal volume V_T listed in the table is not the tidal volume for quiet rest breathing (400–600 mL), since vaping involves suction of ECA through a mouthpiece (see Sections 3.1 and 3.2). Puff time (s) is t_p . Values taken from rough representative averages from data in Figures 1 and 3 of Spindle et al. [31] and also from Soulet et al. [32].

Parameters of vaping topographies.					
Mouth to Lung (MTL)					
Intensity	m_b	V_b	Φ_b	t_p	V_T
Low	2–10 mg	20–100	20–40	2–5	500–1500
Direct to Lung (DTL)					
Intensity	m_b	V_b	Φ_b	t_p	V_T
High	10–40 mg	300–500	100–300	3–6	1000–3000

2.1.2. Demographics and Markets

It is crucial to examine how representative among vapers are the different puff topographies and levels of intensity, something that has varied with time depending on the popularity and availability of different devices. Currently, low-powered devices (mostly but not exclusively closed) are the most representative in the largest and most established markets. As shown in Figure S1 (with credit to [34]), consumer surveys reveal that the overwhelming majority of vapers (90% in the USA and 80% in the UK) utilize low-powered devices (mostly kits for beginners and closed systems) that operate with the low-intensity MTL style, while only a minority use advanced open-tank systems appropriate for the intense DTL style.

2.2. Inhaled and Exhaled E-Cigarette Aerosol (ECA)

ECA is generated by various physicochemical processes: self-nucleated condensation in a super saturated medium initiates immediately once the e-liquid vapor leaves the coil, and the nucleated centers generate small nanometer-scale droplets that grow through coagulation and diffusion (see detailed explanation in [35]). The particulate phase is

made of liquid droplets whose chemical composition closely matches that of the e-liquid: propylene glycol (PG), vegetable glycerin or glycerol (VG), nicotine and water [36], together with a trace level contribution of nanometer-sized metal particles [37]. The gas phase is chemically similar. The aerosol contains nicotine and residues produced from the pyrolysis of the glycols and the flavorings (mainly carbonyls), which can be in either the gas or particulate phase depending on their vapor pressure and volatility [38], with most of the PG evaporating into the gas phase and VG tending to remain in the droplets [36].

Count mean diameter (CMD) distributions of mainstream ECA droplets vary depending on the device, puffing style of users, flavors and nicotine content [35,39]. Droplet number count is heavily dominated by submicron droplets with CMD distributions having either single modes below 100 nm or bimodal forms (one mode well below 100 nm and one in the range 100–300 nm) [35,39–43]. However, particle size grows with increasing coil power [39] and even in low-powered devices the mass distribution is dominated by droplets larger than 600 nm [35]. In fact, Floyd et al. [35] found a third mode around 1 μm that becomes more prominent at increasing power of the tested device while the nanometer-sized modes decrease, likely because higher power involves larger vaporized mass that favors coagulation and scavenging of nanometer-sized droplets by larger droplets.

The inhaled aerosol mass yield depends on the topography parameters given in Table 1. At inhalation of mainstream ECA, instrument measured droplet density numbers are in the range $n_p = 1 - 5 \times 10^9 / \text{cm}^3$ (see [39–43]). Total average ECA droplet numbers of $N_p = 7.6 \times 10^{10}$ were reported by Manigrasso et al. [44] for a tank system using e-liquids with high nicotine content in a 2 s machine puff regime with $V_b = 50$ mL puff volume (N_p decreases 25% with nicotine-free e-liquids). (These machine puff time lapses are different from those reported in Table 1. The former correspond only to inhalation times as instruments aim at simulation of a mouth inhalation, the latter are time lapses in human vapers and thus include inhalation and exhalation.) Using the same experimental design, Fuoco et al. [43] reported an increase of up to 30% for the 4 s machine puff regime. The estimation $N_p \sim 10^{10} - 10^{11}$ is reasonable given a particle number concentration of $n_p \sim 10^9 / \text{cm}^3$ and $V_b = 20 - 100$ mL of low-intensity vaping, with $N_p \sim 10^{12}$ for high-intensity vaping with $V_b = 500$ mL.

Data on the gas/particle phase partition of the aerosol mass yield that m_b is roughly 50% Total Particulate Matter (TPM), 40% PG/VG gas phase, 7% water vapor and <3% nicotine [45], roughly a similar gas/particulate phase partition to that of tobacco smoke [46]. As shown in [36,38], the presence of compounds in gas or PM form depends on their vapor pressure, with PG tending to be gaseous, VG in PM, for nicotine it depends on its Ph, while some aldehydes (e.g., formaldehyde) are most likely in the gas phase.

Values of particle numbers and densities for the exhaled ECA can be estimated by considering its retention by the respiratory system. Compound specific retention percentages were reported by St. Helen et al. [47] for a wide variety of devices and e-liquids: 86% VG, 92% PG and 94% nicotine. Samburova et al. [48] reported 97% total aldehyde retention. These high retention percentages are consistent with the mass distribution of inhaled ECA dominated by larger micron-sized droplets which tend to be efficiently deposited in the upper respiratory tracts [35]. Assuming equal retention rate for the particulate and gas phases, we take as total mass of exhaled aerosol and total numbers of exhaled ECA droplet to be 10% of the values of m_b listed in Table 1 and 10% of the values of $N_p = 6.7 \times 10^{10}$ reported in [44] for a 2 s machine inhalation puff and 50 mL puff volume. Droplet number density of ECA as it is exhaled can be estimated from these values of N_p bearing in mind that the exhaled ECA is now diluted in tidal volumes V_T listed in Table 1 for the various vaping topographies. This yields number densities in the approximate range $n_p = 10^6 - 10^7 \text{ cm}^{-3}$ (lower to higher vaping intensities).

Exhaled ECA dilutes and disperses very fast. Its chemical composition is similar to that of inhaled ECA, in both the gas phase and the droplets [35], with PG and water in the latter evaporating rapidly. Since hyperfine nanometer-sized droplets deposit efficiently by diffusion in the alveolar region and larger micron-sized droplets (which tend to

grow from hygroscopic coagulation [33,35]) deposit by impaction in the upper respiratory tracts [33,39,41,44], the CMD distribution of ECA as it is exhaled should be dominated by modes in intermediate ranges 0.1–0.5 μm . Since there are no ECA measurements at the exhalation point (the vaper's mouth), we can estimate the representative droplet diameter by a rough order of magnitude calculation: assuming an aerosol mass yield of 5 mg of inhaled ECA for a low-powered device and a 90% retention of aerosol mass with 50% made of PM, the total droplet mass of exhaled ECA should be around $M_p = 0.25$ mg. Assuming a 90% retention of inhaled droplets, the total number of exhaled droplets should be $N_p = 7.6 \times 10^9$ droplets (from inhaled numbers in [44]), leading to a median droplet mass of $m_p = M_p/N_p = 3.9 \times 10^{-14}$ gm = $(\pi/6)\rho_p d_p^3$, where ρ_p is the droplets density that we can assume to be close to VG density $\rho_p = 1.3$ gm/cm³, leading to $d_p = 0.38$ μm . Similar order of magnitude values are obtained for the parameters of high-intensity vaping.

The fact that CMD chamber measurements are in the range $d_p = 0.1$ – 0.2 μm can be explained by the fact that detectors are located 1–2 m from the exhalation source, thus measured ECA droplets have already undergone significant degree of dilution and evaporation (as shown in [36], droplets' mass can decrease by one third in just 1 s by evaporation of its PG content). This is consistent with droplet number densities dropping at least two orders of magnitude from $n_p \sim 10^6$ – 10^7 cm⁻³ as they are exhaled to $n_p \sim 10^4$ – 10^5 cm⁻³ at 1 m distance from the emission and further dropping to near background levels $n \sim 10^3$ cm⁻³ at 2 m [49–51].

2.3. Exhaled ECA as a Visual Tracer of Respiratory Fluid Flow

The overwhelmingly submicron droplets that form the particulate phase of ECA have negligible influence on its fluid dynamics, acting essentially as visible tracers or (to a good approximation) as molecular contaminants carried by the fluid. This follows from its basic fluid dynamical characteristic: it is a “single-phase fluid flow” (SFF) system [52,53]. As a consequence, ECA droplets visually mark the actual expiratory flow associated with vaping exhalations (we discuss the optical properties that allow for its visualization in [22]).

Exhaled ECA is just one among numerous gas markers and aerosols in a SFF regime that serve (and are widely used) to visualize expired air [54,55]. This also applies to mainstream exhaled tobacco smoke, whose particulate matter is also made of submicron liquid and solid droplets. In fact, there are studies that have directly used cigarette smoke as a tracer to visualize respiratory airflows [56–58]. Respiratory droplets potentially carried by exhaled ECA would not change its possible role as a tracer of expiratory flows, since, as we show in Section 3.3, these droplets are also overwhelmingly in the submicron range and their numbers are several orders of magnitude fewer than ECA droplets.

Submicron ECA droplets are carried by a fluid made of the gas phase of ECA strongly diluted in exhaled air (in practice, we can think of the carrier fluid as exhaled air at mouth temperature ~ 30 – 35 °C and 80–100% relative humidity). Under such conditions, ECA droplets essentially follow the fluid flow because of their little inertia, as they are well within the Stokes regime with Reynolds numbers $Re_p \ll 1$ and negligibly small relaxation times t_{rel} , the response time of an aerosol particle to adjust to external forces. For $d_p = 0.3$ μm , we get [59]

$$t_{rel} = \frac{\rho_p d_p^2 C_c}{18\mu} \approx 5.3 \times 10^{-6} \text{ sec}, \quad (1)$$

where $\rho_p \sim 1.3$ gm/cm³ (close to VG density), $\mu = 1.895 \times 10^{-5}$ gm/(s cm) the dynamic viscosity of air at 35 °C and $C_c = 1 + (\lambda/d_p)[2.34 + 1.05 \exp(-0.39d_p/\lambda)] \approx 1.4$ is the Cunningham slip factor with $\lambda = 0.066$ μm the mean molecular free path of air.

The relaxation time (1) provides the time scale for a particle released into a fluid with velocity U along a horizontal stream to settle into the fluid velocity (neglecting gravity). In this case (see Chapter 3 of [59]), the velocity of the particle $v_p(t) = U(1 - e^{-t/t_{rel}})$ becomes practically identical to U in about 10^{-5} s (instantaneously in practical terms), thus justifying

the notion of particles simply following the fluid flow with (practically) no influence on its dynamics, (effects that characterize the Stokes regime).

This behavior also occurs for the larger ECA droplets of $d_p \sim 1 \mu\text{m}$ whose relaxation times are $t_{\text{rel}} \sim 10^{-4}$ (since $t_{\text{rel}} \propto d_p^2$). Evidently, these relaxation times are much smaller than macroscopic characteristic times of the carrier fluid (e.g., a 2 s inhalation time or even the tenths of a second the ECA stays in the mouth cavity [33]). The Stokes number is defined as $St = t_{\text{rel}}/t_f$, where t_f is a characteristic fluid time, hence for the exhaled ECA we have $St \ll 1$, which is another criterion to define the Stokes regime and is characteristic of SFF systems.

Evidently, larger droplets (diameters larger than a few μm) are present in particle diameter distributions (of both ECA and respiratory droplets) and such particles should contain a significant portion of the aerosol mass [35], but they are too few in numbers and deviate from the flow following ballistic trajectories, thus do not affect the dynamics of the carrier fluid to consider ECA as a biphasic fluid flow system (as is the case with violent coughs or sneezes, see [60]).

3. Methods: Inferences on Respiratory Droplets Spread by ECA

3.1. Vaping as a Respiratory Process

Tobacco smoke is a valid physical reference for ECA, as it is also an aerosol in a SFF regime characterized by a particulate phase made of predominantly submicron particles with similar particle numbers and diameter distributions [35,41,61] (although the particulate and the gas phases of each aerosol have very different chemical properties). This fact, together with the fact that most vapers are either cigarette smokers or ex-smokers of cigarettes, justifies inferring the respiratory parameters of vaping (especially exhaled volume) from the respiratory parameters of smoking reported in the literature (see reviews in [62,63]; see also a summary of studies in Table S2).

3.1.1. Respiratory Parameters of Smoking

While there is a wide individual diversity in respiratory parameters among smokers, roughly the same three puffing topography patterns identified in Section 2.1 for vaping occur in smoking (with tobacco smoke instead of ECA) [64]. As with vaping, the most common cigarette smoking topography is MTL, an expected outcome since most vapers are either ex-smokers or current smokers of cigarettes. While a sizeable minority of 10–20% of vapers (see Section 2.1.2) follow the DLT style, the vast majority of smokers avoid direct lung inhalation because it is too irritant [65] (and is consistently associated with airways narrowing [64]). In fact, avoidance of the direct lung inhalation of DTL style is very likely an organic response to minimize to a tolerable level the irritant quality of tobacco smoke [64–66].

Regarding its respiratory parameters, cigarette smoking involves a larger percentage of vital capacity than rest breathing at 20–25% [62], although low-intensity inhalators might use on average only 14% [66]. It is extremely likely that these figures apply at least to MTL vaping. Other parameters such as expired tidal volume, puff times and volumes obtained in observational studies are listed in Table S2 (Supplementary Materia), where we use outcomes from references cited in two comprehensive reviews [62,63]. The summary of these outcomes is roughly:

- Puff Volume (volume of the smoke bolus drawn from the cigarette) is 20–70 mL.
- Puffing Time (time to draw the smoke bolus from the cigarette) is ~ 2 s.
- Total smoking time lapse (inhalation, breath hold and exhalation) is ~ 4 –7 s.
- Tidal volume (the volume of the total inhaled/exhaled smoke mixed with air, V_T in Table 1) varies widely between 500 and 1500 mL (with some outliers reaching as low as 300 mL or as high as 2000 mL), but typically group averages are between 700 and 900 mL.

It is worth remarking that puffing times are slightly shorter but roughly comparable to those of MTL vapers, while tidal volumes are 25–30% larger than rest tidal volumes

(400–600 mL), although the measurement of these volumes is subject to at least a 10% error [67] and not all air drawn with the purpose of inhaling smoke is actually inhaled. Most studies report inhaled volumes, but exhalation volumes are roughly comparable (see Table S2), as smoke is highly diluted in air and its retention barely affects volume measurement.

3.1.2. Suction

As opposed to rest breathing, smoking and vaping involve suction: the inward force needed to draw smoke (or ECA) associated with the negative/positive pressure gradient ΔP generated by the diaphragm driven expansion/contraction of the lungs. Airflow resistance follows from the relation between the flow of air volume $Q = dV/dt$ and this pressure gradient, a relation that can be modeled by the following power law (see [68,69])

$$\Delta P = a Q^b, \quad a, b \text{ constants}, \quad (2)$$

where a , b are determined empirically. This power law can be related to fluid dynamics (see discussion in [69]): the constants a and b correlate with fluid density, while the exponent b can be referred to the “classical” flow regimes: $b = 1$ corresponds to laminar flow with Reynolds numbers $Re_f < 10$ (Poiseuille law), $b = 1.75$ to turbulent flow with $Re_f \sim 10,000$ (Blasius law) and $b = 2$ to the “orifice” flow characterized by turbulent flow in narrow pipes and containers.

The theoretical connection with fluid mechanics has motivated airflow resistance measurements in the upper respiratory system that yield values around $b = 1.84$ [68,69] for resting oral and nasal breathing. An excellent fit of this power law relation to the classical orifice flow $b = 2$ was found for a conventional cigarette and two second-generation e-cigarettes by [61], with the e-cigarettes flow resistance a being 3–4 times larger than the conventional cigarette. As a consequence, given the same suction effort (same ΔP), a conventional cigarette yields a puffing flow Q 3–4 times larger than the tested e-cigarettes (second generation). However, vapers can compensate for the higher flow resistance of ECA and draw relatively large aerosol mass with the same suction effort by puffing for longer times (as shown by topography studies). In addition, the laboratory measurements of Sosnowski and Kramek-Romanowska [61] were conducted under idealized conditions and are very likely to vary among the many e-cigarette devices in natural usage conditions.

A factor that distinguishes cigarette smoking from vaping is that the latter involves suction of ECA through a mouthpiece. However, in most of the studies listed in Table S2, the subjects smoked through cigarette holders that are part of the laboratory instrumentation. This makes the listed outcomes more useful to infer respiratory parameters for vapers, at least for those vaping in the MTL style, since these holders are of similar size and shape as the narrow e-cigarette mouthpieces. However, usage of cigarette holders does not seem to introduce significant changes in tidal volume, as can be seen by comparing outcomes from studies that used holders with those who did not in Table S2 (we comment further on the effect of mouthpieces in Section 3.2).

Since MTL is the most common topography among smokers and vapers (most of whom are ex-smokers or current smokers), we can assume that MTL style vaping is characterized by qualitatively similar puffing and respiratory parameters to those listed in Table S2. While some smokers inhale without a mouth hold as in DTL style, this does not seem to involve in them a significantly higher tidal volume, most likely because it can be too irritant [64,66]. The lesser irritant nature of ECA is a plausible explanation for a larger proportion of vapers that can tolerate DTL topography, which means suction of a much larger aerosol mass [32,70] and thus significantly larger puffing and tidal volumes than in MTL style (made easier by usage of high-powered devices). A puff volume of 500 mL can yield under idealized laboratory conditions an inhalation tidal volume close to 3 L [71], which justifies the more plausible values listed in Table 1.

3.2. Mouthpieces, Nose-Clips and the Breathing Route

Mouthpieces (MP) and nose-clips (NC) (to block nasal inspiration) are standard instruments in observational studies, not only those aimed at studying droplet emission, but of respiratory patterns and flows in human subjects. Since the results of these studies can serve as appropriate proxy values to infer droplet emission in vaping, it is important to assess the effects of these instruments in respiratory mechanics. For the purpose of the present article, this issue is interesting because ECA is inhaled in e-cigarettes through mouthpieces (although without obstruction of nasal breathing).

3.2.1. Observational Data on Breathing Through Mouthpieces and Noseclips

Several studies conducted in the 1970s and 1980s [72–76] showed that breathing through MPs and NCs affect all respiratory parameters with respect to unencumbered nose breathing: while tidal volume increases roughly 20% with respect to its normal rest value of 400–600 mL in all studies, inhalation and exhalation times and respiratory frequency are much less affected. It was shown by Weissman et al. [76] that a NC without a MP produces a similar increase of tidal volume but also significant increases of inhalation times (15%) and exhalation times (22%). In two of the studies [73,76], the subjects were in supine position, which yields slightly smaller tidal volumes but does not modify inspiration/expiration times [77].

Besides possible reasons such as the psychological sensorial stimulation of receptors by colder air in mouth inspiration and the stress of breathing through instruments, another possible explanation for the observed change in respiratory parameters of MPs is the change of airflow resistance, for example a 70–90% reduction seen by Weissman et al. [76] brought by the large added mouthpiece dead space (up to 80 mL), while the larger airflow resistance from the standard 17 mm to a narrower 9 mm MP (closer in size to mouthpieces used in vaping) reduced the increase of tidal volume to 11% and inhalation/exhalation times to 9% [76]. Therefore, the MPs of e-cigarettes should produce similar modifications of respiratory parameters as with the narrower MP.

3.2.2. Effects of the Breathing Route

In the studies discussed above, there was no separation between usage of instruments (MP and NC) and oral breathing. Rodenstein, Mercenier and Stanescu [78] conducted several experiments with 14 healthy subjects with the aim of looking separately at the effects of MPs and an NC. Their main result is that changes of respiratory parameters (rough 20% and 10% increase of tidal volume and inhalation/exhalation cycle) are entirely due to the forced oral breathing induced by the NC; in fact, nose occlusion is not even necessary to produce these changes: it is sufficient to simply instruct the subjects to breath through the mouth to observe an increase the tidal volume by a similar proportion as with the use of a NC, from 456 ± 142 to 571 ± 199 mL, although inhalation/exhalation times and other parameters remain almost the same (likely because of breathing without instrumentation).

The physiology behind the effects of the breathing route is similar to the one discussed in the study of pipe and cigarette smokers [79]: changes of respiratory parameters depend on the degree with which subjects are able to maintain air flowing through the nose. These parameters exhibit minor variation as long as this air flow is not occluded and the oropharyngeal isthmus remains closed. The parameters change significantly when nose occlusion separates the soft palate and the tongue and opens the oropharyngeal isthmus to allow air to flow entirely through the mouth. However, after the initial puffing, air flows through both nose and mouth in smoking and vaping (except the mouth puffing style), with the soft palate closing and rising enough to control the oral or nasal flow. While vaping involves usage of a MP, it does not involve nasal occlusion, hence the increase of expired tidal volume with respect to rest breathing (and puffing times with respect to smoking) should be primarily due to suction of ECA.

3.3. Likely Characteristics of Respiratory Droplets Carried by ECA

The discussion in the previous sections has allowed us to infer the characteristics and parameters of the respiratory mechanics of vaping. We need now to identify among respiratory processes the ones that most closely fit these parameters in order to use their available experimental data to infer the capacity of vaping for respiratory droplets emission.

3.3.1. The Right Respiratory Proxy: Mouth Breathing

Intuitively, vaping as a respiratory process should be close to mouth breathing, as both involve a roughly time-symmetric cycle of inspiration/expiration (as opposed to vocalizing, coughing or sneezing). Given the fact that exhaled ECA is a single phase flow (SFF) system (see Section 2.3), another good criterion to relate vaping to mouth breathing is the comparison between their fluid exhalation velocity U_0 and measured analogous velocities in other respiratory processes.

The exhalation velocity U_0 can be roughly inferred qualitatively by considering an exhaled tidal volume of fluid flowing through the respiratory tracts. Considering the respiratory parameters discussed in the previous sections (summarized in Table 1), we can use the simple approximate formula

$$U_0 \approx \frac{V_T}{t_{\text{exh}} A}, \quad (3)$$

where V_T is the expiration tidal volume (in cm^3), t_{exh} is the exhalation time in seconds and A is the combined mouth and nose area (in cm^2), as the fluid carrier of both ECA and tobacco smoke is exhaled through the mouth and nose. From the values listed in Table 1 and Table S2, we have:

- MTL vaping and smoking: $V_T = 500\text{--}1500$ mL and $t_{\text{exh}} = 2\text{--}3$ s, while values for the combined mouth/nose area have been measured as $A = 2\text{--}3$ cm^2 [57].
- DTL Vaping: $V_T = 1500\text{--}3000$ mL with $t_{\text{exh}} \approx 3\text{--}4$ s and $A \approx 3$ cm^2 . Given the large amount of exhaled fluid, we assume longer exhalation times and larger mouth opening area.

From the combination of the parameter values mentioned above, we have

$$U_0 \approx 80 - 375 \frac{\text{cm}}{\text{s}} \quad \text{MTL} \quad U_0 \approx 125 - 500 \frac{\text{cm}}{\text{s}} \quad \text{DTL}, \quad (4)$$

which reinforces the intuitive notion that mouth breathing is the appropriate respiratory proxy for MTL and DTL vaping (and also cigarette smoking), since these estimated exhalation velocities are well within the range of those of exhaled breath in mouth breathing without nose occlusion by NCs [80–82], which have been estimated and measured by various techniques (including Schlieren photography). Exhalation velocities in the most intense DTL vaping regime approach in their upper end the velocities of vocalizing but fall short of those of coughing and sneezing. As a reference, measurements of U_0 using particle image velocimetry resulted in averages of 3.9 m/s for speaking and 11.7 m/s for coughing [83] (measurements in [84] resulted in 6–22 m/s with an average of 11.2 m/s for coughing), while 35 m/s has been estimated for sneezing [85–87].

3.3.2. Data on Droplet Emission from Mouth Breathing

There is an extensive literature on respiratory droplets emitted by mouth breathing at different levels of lung capacity, including rest tidal volume breathing (<20% of vital capacity). We list a selection of these studies in Table 2, as they are the ones that can serve as proxies for vaping and smoking (at least MTL style). In practically all the listed studies, subjects breathed through MPs and NCs, which, as discussed in Section 3.2, involves occlusion of nasal air flow that implies a slightly modified mechanics and about 20–25% larger tidal volume with respect to normal unencumbered breathing.

The fact that emitted respiratory droplets in tidal volumes close to rest breathing are overwhelmingly in the submicron range (as shown by Table 2) implies a very rapid evaporation (0.01 s) that in practice can be considered as instantaneous, with the emitted droplets being overwhelmingly desiccated droplet nuclei made of salt crystals and lipoproteins and being about roughly half their original diameter (see [88]). The exhaled breath will also contain some larger respiratory particles (droplets or nuclei) with $d_r \sim 1\text{--}3\ \mu\text{m}$ that evaporate in timescales of 0.1 s so that (given the exhalation velocities in (4)) they become desiccated nuclei at horizontal distances of 10–30 cm. As a consequence, relative humidity bears negligible influence on the evolution of the bulk of emitted droplets.

While some of the studies in Table 2 were motivated by investigating droplet emission in the context of airborne pathogen contagion (e.g., [89–92]), the motivation of others is to probe various mechanisms of droplet formation [93–98] (see comprehensive discussions and reviews in [86,99,100]), specifically the airway reopening hypothesis of small peripheral airways that normally close following a deep expiration, which was further tested by computerized modeling by Haslbeck et al. [100], who simulated this mechanism of particle formation by rupture of surfactant films involving surface tension. The mechanism was probed by Johnson and Morawska [93] by showing that concentrations of exhaled particles significantly increase with breathing intensities higher than rest tidal volume, but also for fast exhalations but not fast inhalation, while droplet numbers increased up to two orders of magnitude: from $\sim 230/\text{L}$ in tidal volume (0.7 L) to over 1200/L in a breathing maneuver from fractional residual capacity to total lung capacity (see [95]).

The difference in droplet formation between breathing and speaking was examined by Johnson et al. [101]: normal and deep tidal breathing produced submicron distributions related to those of other studies probing the airway reopening mechanism, while speech and cough produced larger diameter modes ($d_r \sim 1\ \mu\text{m}$) with particle formation associated with vocal cord vibrations and aerosolization in the laryngeal region. A third mode of median diameter of $d_r \sim 200\ \mu\text{m}$ was associated with the presence of saliva between the epiglottis and the lips.

Breath holding between inspiration and expiration was found by Johnson and Morawska [93] to significantly reduce concentrations of exhaled droplets in proportion to the breath hold time. The same outcome was found by Holmgren et al. [102] for inspiration to total lung capacity, but droplet numbers increased when the breath hold occurs before inspiration. These outcomes fit predicted effects of gravitational settling in the alveolar region. Since the observations of Johnson and Morawska [93] and Holmgren et al. [102] involved breathing intensity well above tidal volume up to total vital capacity, it is not possible to compare them quantitatively with the breath hold of the MTL style. However, gravitational settling of larger droplets must also occur in the bucal cavity under normal vaping conditions (see [33]), so it is reasonable to assume that reduction of exhaled droplet numbers should also occur at lower intensity in MTL style vaping.

Table 2. Droplet emissions for mouth breathing and tidal volume. The symbols N_r and n_r stand for respiratory particle (droplet or nuclei) number per exhalation and average number density (cm^{-3}). LE, HE, BH, L, and “exh” are Low Emitters, High Emitters, Breath Hold, L and exhalation, while OPC, EM, APS, SMPS and CNC are optical particle counter, electron microscopy, aerodynamic particle sizer, scanning mobility particle sizer and condensation nucleus counter, respectively. Table and figure numbers (4th column) correspond to articles cited in the Table. The subjects in all studies (save possibly the study by Johnson and Morawska [93]) breathed through a mouthpiece wearing a nose clip.

Study Authors and Reference	Droplet Numbers N_r , Density n_r and Diameters d_r	Subjects	Comments and Technique
Papineni and Rosenthal [89]	Mean $N_r = 12.5/\text{L}$, ($<1 \mu\text{m}$) Mean $N_r = 1.9/\text{L}$, ($>1 \mu\text{m}$)	5 healthy	Table 2 OPC, EM
Johnson and Morawska [93]	$n_r < 0.25/\text{cm}^3$ (V_T) up to $n_r = 2.5/\text{cm}^3$ (deep)	17 healthy ages 19–60	Figures 3 and 7. BH decreases droplet numbers APS
Morawska et al. [94]	Mean $N_r = 98/\text{L}$ Mean $d_r = 0.8 \mu\text{m}$	15 healthy ages < 35	nose inhalation and mouth exhalation APS
Almstrand et al. [95]	$N_r = 230/\text{L}$, (18–1000)/L $d_r = 0.3\text{--}0.4 \mu\text{m}$ 98% $d_r < 1.0 \mu\text{m}$	10 healthy ages 29–69	Tidal Volume Tables 2 and 3 OPC
Holmgren et al. [96]	Median $n_r = 3.1$ (0.6–82)/ cm^3 $\bar{d}_r = 0.07 \mu\text{m}$ $V_{\text{ex}} = 351\text{--}1701 \text{cm}^3$	16 healthy	Tables 3 and 4 Two super emitters SMPS
Schwarz et al. [97]	$N_r \approx 10\text{--}50/\text{exh}$ Median $d_r = 0.28 \mu\text{m}$	21 healthy (4 smokers)	Close to V_T $V_T/V_C \approx 0.2$ CNC
Fabian et al. [90]	GMean $N_r = 7.4/\text{L}$ LE GMean $N_r = 3500/\text{L}$ HE 82% $d_r = 0.3\text{--}0.5 \mu\text{m}$	19 subjects (7 asthmatic)	4 HE Table 1 OPC
Wurie et al. [91]	Median $N_r = 38.3$ (3.3–1456)/L 90% $N_r < 150/\text{L}$, LE 99.9% $d_r < 1.0 \mu\text{m}$ 75% $d_r < 0.5 \mu\text{m}$	79 healthy (14 asthmatic)	4–19% high emitters follow up of subjects OPC
Schwarz et al. [98]	$N_r \approx 10/\text{exh}$ LE up to $N_r \approx 1000/\text{exh}$ HE Median $d_r = 0.3 \mu\text{m}$	29 healthy (13 smokers) 28 COPD 10 asthmatic	Figures 2 and 4 Close to V_T $V_T/V_C \approx 0.2$ CNC
Asadi et al. [92]	$N_r \approx 1/\text{s}$ $d_r = 0.75\text{--}1.0 \mu\text{m}$ $n_r < 0.1/\text{cm}^3$	48 healthy age 18–45 10 asthmatic	Figure 5 much larger in speech than in breathing APS

4. Hydrodynamical Modeling of Direct Exposure

In the previous sections, we infer the submicron characteristics and rate of emission of respiratory droplets expected to be carried by exhaled ECA. We need to estimate now how far can these respiratory droplets be carried to evaluate the distance for direct exposure of bystanders to pathogens potentially carried by these droplets

Exhaled ECA is injected into surrounding air a given horizontal distance roughly in the direction of the exhaled flow. Since it involves a finite fluid mass of a SFF aerosol during a finite injection time (exhalation time), the appropriate dynamical model for it is a turbulent puff with a starting momentum dominated jet that lasts while the fluid injection is on (see [103–109]). A schematic description of this system is furnished by Figure 1. We are not concerned with the few larger ECA or respiratory particles (diameters d_p , $d_r \sim$

1–5 μm and over) that initially follow the fluid stream but (depending on their size) exit the main flow to follow ballistic trajectories until they either deposit on surfaces, settle on the ground or evaporate (see [60,86]).

Given the distance and time dispersion scales (<3 m and <2–3 min), we can approximate the ECA as an airflow at constant atmospheric pressure, air density and dynamical viscosity ρ_a and μ . For a jet source (vaper’s mouth) approximated as an orifice of 1.5–3 cm² area [57] (diameter $d_0 = 1.25$ – 1.75 cm) and initial velocities U_0 given by (4), exhalation fluid Reynolds numbers $Re_f = (\rho_a/\mu)U_0d_0 = 600$ – 4400 are in the transition between laminar and turbulent, values well below the high Reynolds numbers expected near a jet source [103,104], but we are mostly concerned with the jet evolution and displacement (penetration) along horizontal distances $z \gg d_0$. Other parameters to consider are the injection time $t_{\text{exh}} = 2$ – 5 s and a temperature gradient from exhalation (initial) $T = 30^\circ$ – 35° C (mouth temperature) into an assumed $T = 20^\circ$ C for the surrounding air. For such values and scales, the starting jet can be regarded as isothermal with thermal buoyancy becoming relevant only in the puff stage (see [107,108]).

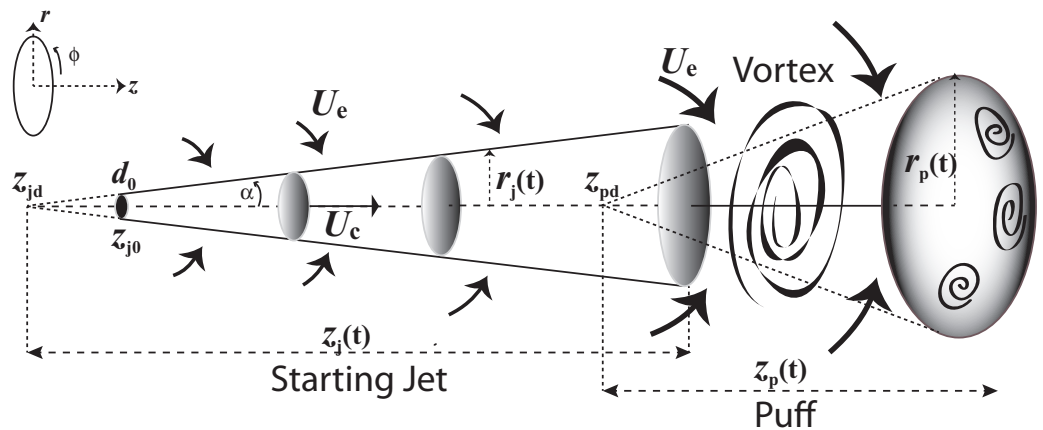


Figure 1. Puff and initial Jet with axial symmetry. The starting jet is propelled by linear momentum parallel to the centerline velocity U_c ; the arrows above and below represent the entrainment velocity mixing surrounding air with the carrier fluid. As the fluid injection terminates (end of exhalation), the entrained air makes about 40% of the fluid mass transition into an ellipsoidal puff through highly turbulent vortex structures. At this point, the puff is likely to disperse rapidly as horizontal displacement velocities are comparable to velocity fluctuations characterizing high turbulence and thermal buoyancy.

It is well known (see [103,104,110,111]) that statistically steady and unsteady jet/puff systems can be well approximated by analytic solutions of the Navier–Stokes and conservation equations (assuming incompressible fluids) with axial symmetry and a self similar profile for the average centerline and radial components of the velocity field in cylindrical coordinates $\vec{U} = [U_z, U_r, U_\phi]$ (see Figure 1)

$$U_z = U_c(t) f(\eta), \quad U_r = U_c(t) g(\eta), \quad U_\phi = 0, \tag{5}$$

where $f(\eta)$, $g(\eta)$ are empiric Gaussian or polynomial functions of the self similar variable $\eta = r/z$, while the centerline velocity is $U_c = U_z$ for $r = 0$ along the z axis, hence $f(\eta)$, $g(\eta)$ must satisfy $U_z = U_c$ and $U_r = 0$ at $r = 0$. In fact, for statistically steady jets (as we are assuming) the axial and radial similarity functions $f(\eta)$ and $g(\eta)$ satisfy [111]

$$g(\eta) = \eta f(\eta) - \frac{1}{\eta} \int_0^\eta \bar{\eta} f(\bar{\eta}) d\bar{\eta}, \tag{6}$$

so that $g(\eta)$ can be obtained from an empiric choice for $f(\eta)$ (see examples in [86,103–109]). The assumptions we make (statistically steady and axially symmetric self similar pro-

file) imply that the jet/puff system fulfills the conservation of linear specific momentum $Q = V_{pen} U_c$ (puff) and force $\dot{Q} = (d/dt)(V_{pen} U_c)$ (jet) where V_{pen} is the penetration volume [103,109], hence $Q = Q_0$, $\dot{Q} = \dot{Q}_0$ for an initial time $t = t_0$. The stream wise centerline penetration distance and velocity for the jet and puff stages can be given by [109]:

$$\text{Starting Jet} \quad z_j(t) - z_{j0} = C_{jz} (\dot{Q}_0 U_0)^{1/4} (t - t_{j0})^{1/2}, \quad r_j(t) = C_{jr} z_j(t), \quad (7)$$

$$U_{jc} = \frac{dz_j}{dt} = \frac{C_{jz}^2 (\dot{Q}_0 U_0)^{1/2}}{2(z - z_{j0})}, \quad (8)$$

$$\text{Puff Stage} \quad z_p(t) - z_{pd} = C_{pz} (Q_0 U_0)^{1/4} (t - t_{p0})^{1/4}, \quad r_p(t) = C_{pr} z_p(t), \quad (9)$$

$$U_{pc} = \frac{dz_p}{dt} = \frac{C_{pz}^4 Q_0 U_0}{4(z - z_{pd})^3}, \quad (10)$$

where the constants $C_{jz}, C_{jr}, C_{pz}, C_{pr}$ are empirically determined, z_{j0} is the z coordinate value of the ejection orifice and z_{pd} is the virtual origins of the puff (see Figure 2), which is an appropriate parameter to separate the starting jet and puff stages even though it lies within the starting jet region (see the detailed explanation in [109]). In addition, notice that the direct proportionality of the radial and axial displacements, $r(t)$ and $z(t)$, for the jet and puff regimes (through C_{jr}, C_{pr}) implies the conical shape depicted in Figure 1, with a distinct, but constant, radial dispersion angle α for each stage.

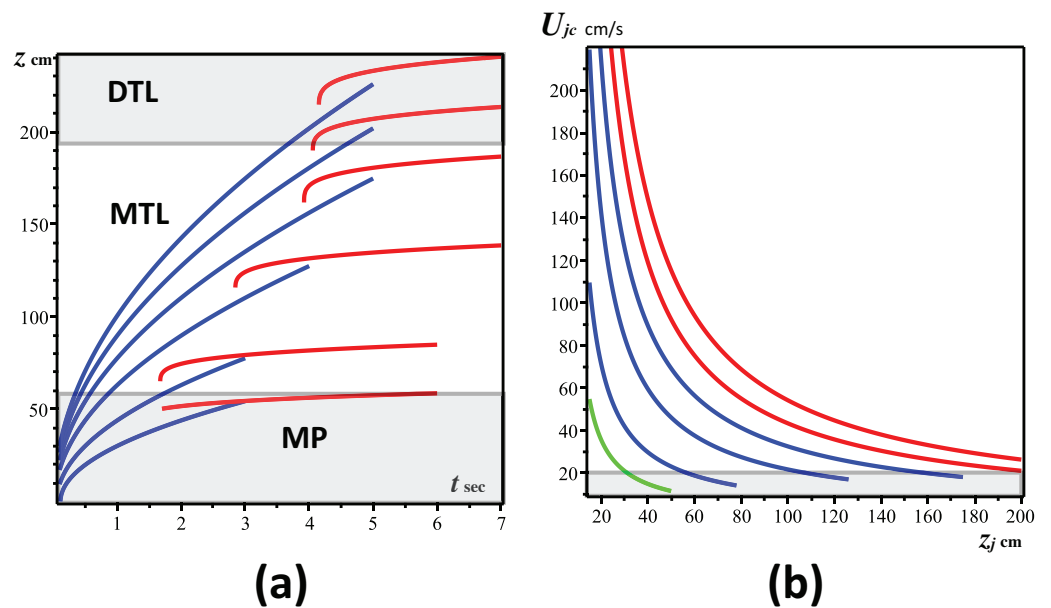


Figure 2. Jet/Puff horizontal displacement and centerline velocity. (a) The displacement z_{jc} of the starting jet (blue) and z_{pc} of the puff (red) as functions of time (Equations (7)–(10)), for the three vaping topographies described in Section 2.1: DTL (Direct to Lung), MTL (Mouth to Lung) and MP (Mouth Puffing). We assumed as injection (exhalation times) 3, 4 and 5 s. The initial velocities from bottom to top are $U_0 = 50, 100, 200, 300, 400, 500$ cm/s. (b) The centerline velocities U_{jc} for the starting jet (Equation (8)), as functions of the horizontal displacement z_{jc} during the injection times and initial velocities of (a) (green for MP, blue for MTL and red for DTL). Notice that once injection stops the jet has reached velocities $\sim 15\text{--}20$ cm/s comparable to those of indoor air currents (bottom rectangle in (b)) and evolves into a puff. Computations and graphs were made with the software package Maple [112]. Worksheets are available through email request to the corresponding author.

For the axial geometry of the jet/puff system under consideration, we have $Q_0 U_0 = \pi d_0^2 U_0 / (8C_{pr}^2)$ and $\dot{Q}_0 U_0 = (3\pi/4)d_0^2 U_0^2$. Following the distinction in Tables 1 and 2 of [109] (see also [109]) between starting and interrupted jets that are, respectively, applica-

ble to our jet and puff stages, we choose the following numerical values for the constants in (7)–(10):

$$C_{jz} = 2.8, \quad C_{jr} = 0.10 - 0.15, \quad z_{j0} = d_0 / (2C_{jr}), \quad (11)$$

$$C_{pz} = 2.6, \quad C_{pr} = 0.18 - 0.29, \quad z_{pd} = z_j(t_{\text{exh}}) - 8.5d_0, \quad (12)$$

where the time t_{pd} and position of the puff virtual origin z_{pd} are determined numerically from (7) by the condition $z_j(t_{pd}) = z_{pd}$ (see [109]).

The values of C_{jr} , C_{pr} above indicate for the jet stage a highly collimated directional evolution with a narrow angle of radial dispersion $\alpha = \arctan C_{jr} \sim 6 - 9^\circ$, while for the puff stage we have a wider radial dispersion $\alpha = \arctan C_{pr} \sim 12 - 16^\circ$ (these angles roughly fit observational data on radial dispersion of mouth breathing, see [57,80–82]). Therefore, since the jet stage is better approximated by an axially symmetric statistically steady jet, this collimated shape implies that the axial displacement is far more relevant than the narrow radial displacement to assess the distance and direction of direct exposure to possibly transported pathogens through vaping exhalations. From the dynamical Equations (7)–(10) with the parameter values in (11)–(12), we display in Section 5.2 the horizontal distance and jet/puff velocities characterizing direct exposure.

Vapers often exhale at a downward angle, typically $\gamma \sim \alpha - 2\alpha$ ($10 - 20^\circ$), thus reducing the horizontal penetration scope of the starting jet by a factor $\cos \gamma$. However, it is this downward exhalation angle (and not so much the radial dispersion) that (under normal natural ventilation) can expose children to the exhaled jet due to their smaller height, but only if they are located in a direction close to that of the jet (see Section 5.3). For the puff stage, the radial dispersion angle is much wider, but at this stage the simple axially symmetric steady state model begins to break down due to thermal buoyancy, turbulence and large flow of surrounding air entrainment, all of which causes a slow puff motion and a rapid dispersion of ECA and the droplets or respiratory particles it might carry. As we show in Section 5.3, the qualitative description of the sharp directional collimation of the jet stage and wider dispersion of a slow unstable puff are corroborated by photographs and videos of actual vaping exhalations by human vapers.

5. Results

5.1. Respiratory Droplets Emission

From the evidence and data examined in Section 3, it is plausible to assume that droplet emission in smoking and vaping (at least MTL style) can be reasonably inferred from outcomes of studies in Table 2 with comparable exhaled tidal volumes (see Table S2), including outcomes of studies mentioned previously that examined breath holds.

The studies we summarized and listed in Table 2 only involve mouth breathing, but they share some common respiratory features with vaping and smoking: oral inspiration with usage of MPs (in vaping), as well as qualitatively similar exhalation velocities and respiratory parameters, namely inhalation/exhalation times and tidal volumes. However, there are also differences: smoking and vaping do not involve the nose occlusion of these experiments, but involve suction which the subjects of the latter experiments did not experience. While the absence of NCs would imply a tidal volume very close to rest values in MTL smoking and vaping, this absence is compensated by the increase due to the need to overcome airflow resistance through suction. The decrease of droplet emission from the mouth/oropharynx hold in MTL topography (absent in normal breathing) was a detected outcome in two of the studies listed in Table 2. We have then the following inferences regarding emission of respiratory droplets:

- **MTL vaping and smoking** (and even DTL vaping not involving deep inspiration). The outcomes displayed in Table S2 and Table 2 suggest that exhaled respiratory particles (droplets or nuclei) in mean tidal volumes $V_T = 700\text{--}900\text{ cm}^3$ are overwhelmingly in the submicron range (typically peaking at $d_r = 0.3\text{--}0.8\text{ }\mu\text{m}$), with respiratory particle number densities well below $n_r = 1\text{ cm}^{-3}$ and a small rate of droplet emission. Assum-

ing $V_T = 0.75$ L, we have $N_r = 6$ –200 per exhalation. Since the distribution of N_r in the 10 outcomes listed in Table 2 is strongly skewed towards the range $N_r < 30$ with only three studies reporting $N_r > 150$, the median value $N_r = 40$ and median deviation 67.28 provide a more representative description than the mean value $N_r = 79.82$ and standard deviation 74.66. We also assume that the wide individual variation reported in these respiratory studies should also apply to vaping, including the existence of a small minority of outlier individuals that can be thought of as “super emitters” reaching over $N_r \sim 500$ –1000 per exhalation.

- **DTL vaping.** It involves a spectrum of deeper respiratory intensity than MTL vaping and thus should involve a higher rate of droplet emission. A reasonable estimation of emitted droplets in the DTL regime is furnished by the intense DTL (2–3 L exhalation) breathing at fractional residual capacity in [95] and by high end emitters in [90,98], leading to possible emission rates approaching 1000/L. However, this style of vaping is practiced by a small minority of vapers (roughly 10–20%, see Figure S1), while extreme vaping with big clouds (the so-called “cloud chasers”) is even less frequently practiced in competitions or exhibitions. Evidently, this type of extreme vaping cannot be sustained for long periods and is not representative even of DTL vapers.

While the inferred droplet numbers in the upper end of high-intensity DTL vaping can be comparable with low end numbers for vocalizing, the latter involves modes with larger mean droplet diameters because of distinct droplet generation processes (see [92,94,101]).

5.2. Distance for Direct Exposure

Direct exposure to respiratory droplets carried by exhaled ECA can be inferred from the horizontal displacement or penetration distance of the jet/puff system whose dynamics follows from Equations (7)–(10) with the parameter values in (11)–(12). We used the algebraic computing package Maple [112] to plot in Figure 2 the analytic expressions for the displacement distances and centerline velocities for assorted values of initial exhalation velocities U_0 corresponding to the vaping intensities we considered (the Maple worksheets used for the graphs are available through email request to the corresponding author).

Notice that the maximal penetration goes beyond that afforded by the momentum thrust of the starting jet, with the puff further evolving at lesser speeds. Horizontal penetration varies from 0.5 m for Mouth Puffing ($U_0 = 0.5$ m/s) through the range 0.6–2.0 m for the MTL regime ($U_0 = 0.5$ –3.75 m/s) to beyond 2 m for the higher-intensity DTL regime ($U_0 = 1.5$ –5 m/s). Centerline velocity drops to about 0.2 m/s at different times and distances when fluid injection stops in all cases.

Given its short time duration and close distance scope of the momentum thrust jet, the analytic model (7)–(8) remains a reasonably good approximation to infer the necessary distance to minimize the risk of direct exposure of bystanders to respiratory droplets. As the jet evolves while fluid is injected, there is increasing entrainment from the surrounding air at velocity $U_e \propto U_r$, with entrained air reaching about 40% of the jet mass at the end of injection in the transition towards the puff (around its virtual origin, see [107,108]). Since there are airflow currents of ~ 10 cm/s (and up to 25 cm/s) even in still air in home environments with natural ventilation [113,114], at this stage the puff formation can be easily destabilized by vortex motion generated through turbulent mixing from the large velocity fluctuations produced by the entrainment (see details in [115,116]).

Turbulence and thermal buoyancy become important factors when there is human motion or walking [117], or in microenvironments with mechanical ventilation (mixed or displaced), resulting in a faster disruption and dispersion of the slow moving puff, carrying the submicron ECA and respiratory droplets along the air flow. In general, submicron droplets exhaled at the velocities under consideration can remain buoyant for several hours, with mixing ventilation tending to uniformly spread them, whereas directed ventilation tends to stratify them along different temperature layers (see comprehensive treatment in [118–120]). In all cases, there is a risk of indirect contagion by exposure to these droplets. The detailed description of droplet dispersion after the puff is disrupted is a complicated

process that requires computational techniques that are beyond the scope of this paper (see comprehensive analysis in [116]).

5.3. Comparison with Human Vapers

It is important to examine if real life vaping jet/puff systems are well described by the approximation afforded by the simplified hydrodynamical model introduced in Section 4, whose characteristics and distance spread predictions are discussed in Section 5.2 and plotted in Figure 2. To look at this matter, we examine in this section photographs of vaping jet/puff systems produced by actual vapers. These photographs are frames of videoclips available as Supplementary Material SM(3).

5.3.1. DTL Vaping

The evolution of a vaping jet/puff system for a vaper following the DTL style can be appreciated in the sequence of frames displayed in Figure 3. While this style is followed by a minority of vapers (see Section 2.1.2), its large volume of exhaled air and ECA and large distance spread make it suitable to illustrate the evolution of the jet/puff system associated with vaping. Figure 3 contains five images corresponding to the stages of jet/puff formation and evolution in a sequence given by the following time frames from top to bottom (the filmed sequence is available in Supplementary Material SM(3))

First Frame. The starting jet thrust by the linear momentum of the exhalation has a rough conical shape with dispersion angle comparable to $\alpha \sim 15^\circ$, as described in Section 5.2 and depicted in Figure 1.

Second Frame. As more ECA and exhaled air are injected, the shape of the frontal development of the starting jet becomes deformed by entrainment of surrounding air, which initiates the formation of a turbulent vortex. The jet areas close to the injection source (vaper's mouth) remains close to the initial conical shape.

Third Frame. Entrainment from surrounding air generates more turbulent mixing, giving rise to the slow formation of a puff as a deformed ellipsoidal shape that slowly separates from the fully developed starting jet, since fluid and ECA injection continues.

Fourth Frame. As the injection wanes, the starting jet weakens, gradually losing its straight conical shape. The puff becomes fully developed and evolves forward, giving rise to more air entrainment and turbulent mixing.

Fifth Frame. As injection stops, the starting jet is gone and the puff structure begins to disperse.

As shown by the frames depicted in Figure 3 and in the video from where this sequence was taken (see video DTL1 in SM(3)), the simple hydrodynamical model presented and discussed in Sections 4 and 5.2 provides a reasonably good approximation to real life vaping, at least up the fourth frame before the final dispersion of the puff when injection ends (this is also true for MTL vaping with a tank device as we show further ahead). Evidently, the horizontally thrust jet/puff system generated by this vaper (following DTL vaping style) reaches over 2 m of horizontal displacement, which up the puff dispersion final stage remains quite directionally collimated. This corresponds to the upper displacement curves in Figure 2, indicating a probable exhalation velocity of $U_0 \sim 4\text{--}5$ m/s and total fluid injection of over 2 L. However, not all vapers doing DTL style thrust the jet/puff system such large distance spreads and injected fluid volumes, since these parameters should also depend on the lung capacity of the vaper, which varies in direct proportion to body size. The vaper of Figure 3 has a large lung capacity, as he is 1.86 m tall and weighs 110 kg. In the video DTL2 in SM(3), his vaping exhalation is compared to that of a vaper 1.70 m tall weighing 74 kg, whose jet/puff system has a much shorter spread barely surpassing 1.5 m, corresponding (from the results in Figure 2) to probable exhalation velocity $U_0 \sim 2.5$ m/s and total fluid injection of 1.5 L.



Figure 3. Formation and evolution of the vaping jet/puff system. The images denote from top to bottom a sequence of time frames of a vaping jet/puff system associated with the intense DTL style. Each frame is explained in the main text. The video footage is available in SM(3)

5.3.2. MTL Vapers

The jet/puff system exhaled by vapers following the MTL styles exhibits the same stage evolution described in Figure 3, although exhalations produced by low-powered devices involve significantly less fluid injection (and typically lower injection times), thus producing smaller horizontal distance spread, as well as more affectation by external air entrainment that produces a smaller and easier to dispersed puff. All this is corroborated by Figures 4 and 5, which, respectively, depict the horizontal and downward thrust exhalations by MTL vaping with two electronic cigarettes: an open-tank device (Geekvape Aegis X, 40–60 watts) and a low-powered closed “pod” device (Innokin Endura, 10 watts).

Figure 4 depicts the evolution stage for horizontal exhalation of MTL vaping, in a stage equivalent to the fourth frame of Figure 3 (top down), for the tank (top) and pod devices (bottom); both are frames taken from the video MTL1 available in Supplementary Material SM(3). The exhalation produced by the tank device (top) is a smaller scale version of the DTL exhalation depicted in Figure 3 and videos DTL1 and DTL2 of SM(3) (the same tank device can also be used for DTL vaping), displaying a fully formed puff with a waning fluid injection, reaching horizontal distance spread under 1.2 m, thus probably corresponding to approximately $U_0 \sim 1.5$ m/s and total fluid injection of 1 L. As shown by the first exhalation in video MTL1 of SM(3), the distance extension of the film is sufficient to capture how the puff disperses upwards due to thermal buoyancy (while the camera was unable to capture this upward thrust in video DTL1 of SM(3)).

In the exhalation produced by the low-powered device displayed at the bottom of Figure 4, only the starting jet is visible, reaching about 0.7 m, corresponding to lower displacement curves in Figure 3 (likely $U_0 \sim 1$ m/s and total fluid injection of 0.7 L). As shown in the second and third exhalation of video MTL1 of SM(3), as the fluid injection wanes, external air entrainment rapidly disperses the incipient puff. Figure 5 considers the same devices as in Figure 4, but for an exhalation thrust downwards (however, video footage MTL2 of SM(3) is only available for the tank system). As the puff forms, it rapidly settles on the ground without dispersing upwards, most likely because of the deposition of most ECA droplets. The downward exhalation for the low-powered device (not displayed in video) is practically identical to that of the horizontal one, with an even more rapid dispersion of the puff at the end of the fluid injection.

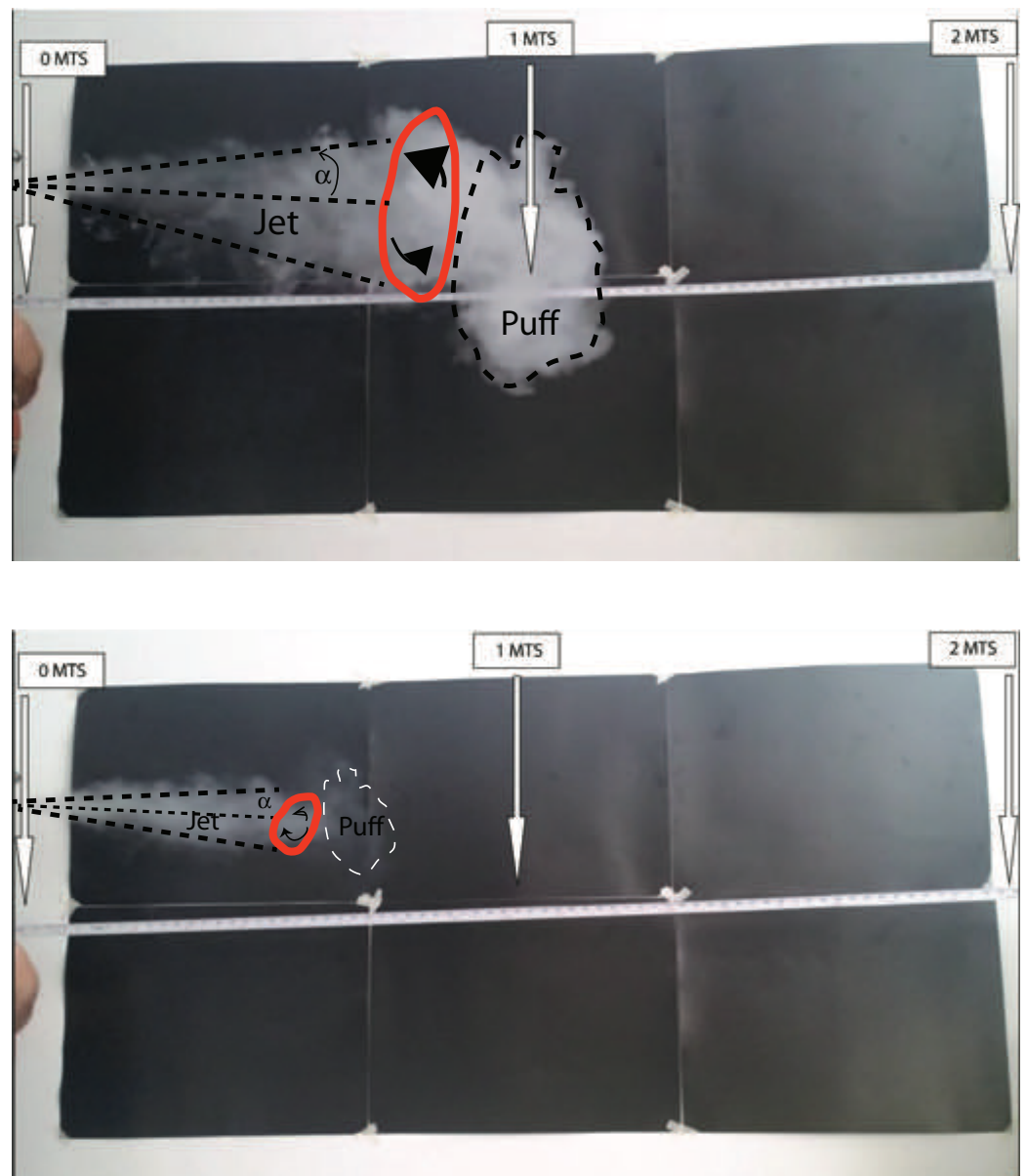


Figure 4. The vaping jet/puff system: MTL style, horizontal exhalation. Top and bottom figures, respectively, depict the jet/puff system exhaled by the same vaper using a tank system and a low-powered pod. Turbulent vortex is marked in red. The frames correspond to an evolution stage equivalent to the fourth frame (top down) of Figure 3. Video footage corresponding to these frames is available in the Supplementary Materials SM(3). See details in the main text.

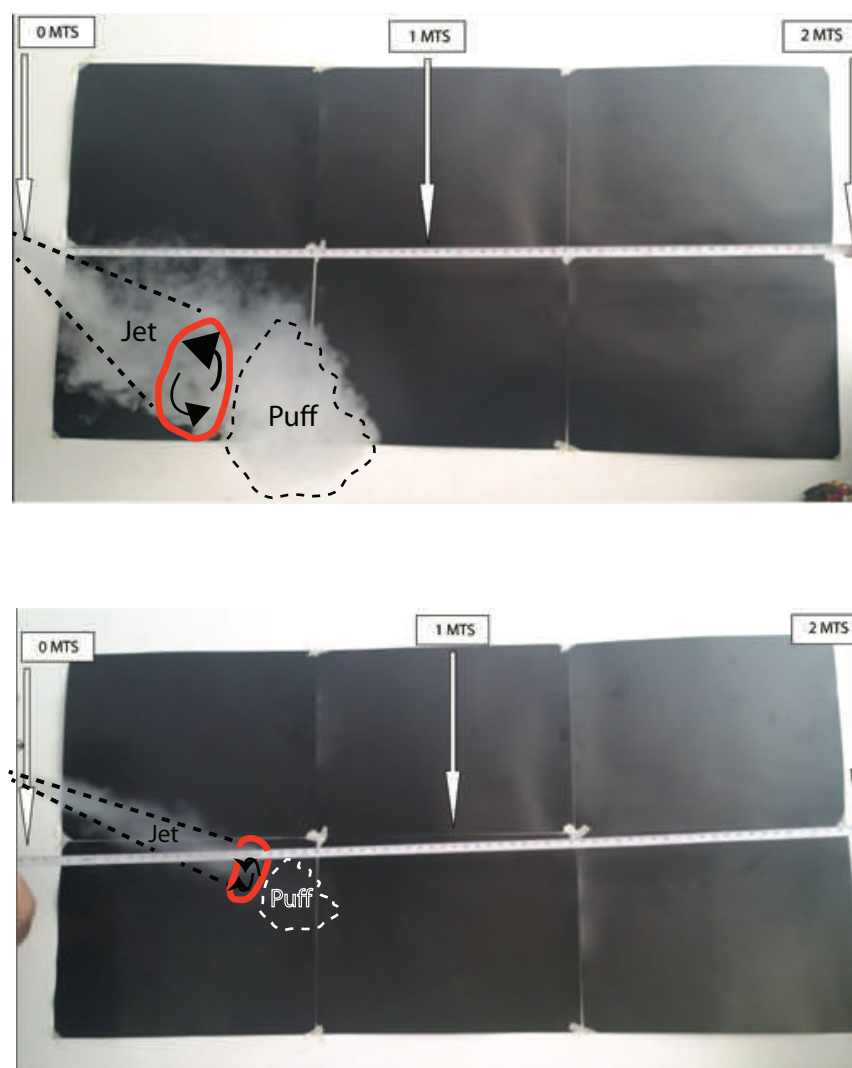


Figure 5. The vaping jet/puff system: MTL style, downward exhalation. Similar to Figure 4 with the jet/puff system thrust downward. See details in the main text. Notice that because of their shorter height children or pets standing at 1 m distance from the vaper using a tank device might be exposed to ECA.

6. Limitations, Final Discussion and Conclusions

We present in this paper a comprehensive analysis and theoretical modeling of the plausibility, scope and risk for pathogen (including SARS-CoV-2 virus) contagion through direct and indirect exposure to respiratory droplets that would be carried by ECA (e-cigarette aerosol) exhaled by vapers. A summary that outlines the methodological structure and obtained results of the article is provided in the Introduction.

6.1. Limitations

6.1.1. Lack of Empiric Data

It is important to openly recognize the main limitation of this study: the lack of experimental and observational data on respiratory droplets carried by exhaled ECA. It is quite plausible that emission of these droplets should occur, as exhaled ECA is an expiratory activity, but without empiric data any quantitative assessment of its nature and scope must necessarily be inferred or estimated indirectly, either through theoretical speculation from the physical and chemical properties of ECA or through extrapolation from available data on other expiratory activities that can serve as reasonable proxies for vaping. The need to provide the best possible and self consistent inference on this missing

data explains and justifies the length of the present study: data availability would render several sections (for example, Sections 3.1–3.3) redundant or drastically shortened and kept only for comparative reference.

6.1.2. Simplification of Vaping Styles

The classification of puffing topographies in two separate mutually exclusive categories (MTL and DTL) that we present in Section 2.1 roughly conveys the two main vaping styles, but e-cigarettes are a rapidly changing technology and thus this simplified approach cannot capture the full range and scope of individual vaping habits.

6.1.3. Oversimplification of Infective Parameters and Individual Variability

We remark that the ranges of numerical values we obtained of emitted droplets possibly emitted by vaping are rough average estimates gathered from outcomes reported in breathing studies (listed in Table 2) involving a wide variety of subjects, including both healthy subjects and individuals affected by respiratory conditions (not by SARS-CoV-2). We did not consider the small minority of outlier individuals who are super spreaders emitting significantly larger numbers of droplets [92]. We also simply considered droplet emission, disregarding the specification of a specific pathogen. Evidently, this oversimplification disregards important known facts, for example droplet characteristics vary among pathogens and between healthy and infected subjects [90,91].

In fact, numerous aspects associated with the spreading and infection details of the SARS-CoV-2 virus remain uncertain and subject to large (often unexplained) individual and environmental variability (a good summary of these uncertainties is found in [13–16]). However, in order to be able to model a possible (previously unexplored) route of droplet transmission and possible infection, it is necessary and unavoidable to simplify this complexity and lack of data to obtain plausible order of magnitude estimates that can be verified once empiric evidence is available.

6.1.4. Oversimplification of Droplet Dynamics

Since respiratory droplets carried by exhaled ECA are expected to be overwhelmingly submicron, and thus carried by the fluid flow, the simple dynamical modeling of a starting jet followed by an unstable puff (Section 4) is sufficient to estimate direct exposure distances (this is corroborated in Section 5.3 by comparison with photographs and videos of actual vapers). However, we recognize its limitations: it is strictly valid for a jet/puff system emitted by a motionless vaper in typical indoor conditions with idealized natural ventilation. Evidently, estimating the fluid flows that determine this exposure (and indirect exposure by dispersing droplets) in less idealized conditions requires a more realistic description using computational methods of fluid mechanics to incorporate effects of turbulence and thermal buoyancy, as well as air currents from ventilation or motion. Rather, we examined global volume exposure in a separate article through a risk model not involving fluid dynamics described [22]. It is important to mention that this simplification of the dynamics is harder to justify for expiratory activities such as coughing or sneezing, as the latter involve larger ejection velocities and a much wider spectrum of droplet diameters that includes significant number of large supermicron droplets (significant numbers of droplets with diameters 1–10 μm and even $>100 \mu\text{m}$) whose effect on the dynamics of the carrier fluid cannot be neglected (these are strictly speaking multiphase flows [52,60,87]).

6.2. Safety Considerations

6.2.1. Respiratory Flow Visualization

As opposed to other respiratory activities (speaking, singing, coughing and sneezing), the involved respiratory flow of ECA is visible because the carried submicron droplets (ECA and respiratory) act effectively as visual tracers of the carrier fluid (see Section 2.3 and further details in [22]). Besides the evident psychological dimension of this flow visualization, there are safety implications: vapers and those surrounding them have a

clear, instinctive and immediate delineation of the flow's horizontal distance reach and spreading direction along the exhaled jet. From the outcomes of our hydrodynamical analysis (Section 5.2), we can recommend as a basic safety measure to avoid direct exposure (irrespective of face mask wearing) by keeping a 2 m distance away from the vaper (when vaping) in the direction of the visible jet. In other directions, the exposure would be indirect, but nevertheless it is prudent to maintain 2 m of separation in all directions from anyone vaping when not wearing a face mask. Notice that these recommended safety measures coincide with the standard social separation recommendations adopted worldwide [121]. Since vapers often thrust their jets in varying downward angles, children and pets might be exposed (because of their shorter height) at distances and positions that could be safe for adults. While vaping starting jets are quite collimated, and thus involve direct exposure mostly in the jet direction, ventilation and motion of the vapors might disperse the emissions in other directions. However, as emphasized above, the fact that these emissions are visible is a valuable safety feature that allows bystanders to avoid exposure.

6.2.2. Final Conclusions

This article is the first comprehensive attempt (as far as we are aware) to assess the plausibility and distance range of possible transport by exhaled ECA of respiratory droplets potentially carrying pathogens (including the SARS-CoV-2 virus). Given the lack of empiric data on this phenomenon, we utilized data from respiratory parameters of cigarette smoking and droplet emission from mouth breathing, both considered as valid proxies for vaping exhalations. As far as we are aware, this is the first study that examines vaping exhalations as hydrodynamical flows. Our results can provide useful guidelines to address the possible scope of vaping exhalations in assessing risks of contagion of infectious disease in shared indoor spaces. In other studies, we examined actual contagion risks and public policy implications (see [22,23]). Setting aside harms from environmental tobacco smoke unrelated to COVID-19, these results also apply to sharing an indoor space with a smoker.

Supplementary Materials: The following are available at <https://www.mdpi.com/article/10.3390/app11146355/s1>, Figure SM(1), Usage of different classes of e-cigarette devices in the US and UK markets. Table SM(2), Respiratory parameters of cigarette smoking. SM(3) contains videoclips DTL1, DTL2 for Figure 3 and MTL1, MTL2 for Figures 4 and 5.

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Informed Consent Statement: Informed consent was obtained from all subjects involved in the study.

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Conflicts of Interest: R.A.S. has no competing interests to declare.

List of Abbreviations and Symbols

Acronyms and Abbreviations

ECA,	E-Cigarette Aerosol
SARS-CoV-2	Severe acute respiratory syndrome coronavirus 2
COVID-19	Coronavirus disease 2019
WHO	World Health Organization
CDC	Centers for Disease Control and Prevention of the USA
MTL	Mouth to Lung (vaping style)
DTL	Direct to Lung (vaping style)
PG	Propylene Glycol
VG	Glycerol or Vegetable Glycerine
SFF	Single-Phase Fluid Flow
PM	ECA Particulate Matter
TPM	ECA Total Particulate Matter
MP	Mouth Piece
NC	Nose Clip

Units

L	liters
mL	milliliters
m	meters
cm	centimeters
mm	millimeters
μm	micrometers
nm	nanometers
mg	milligrams
μg	micrograms
s	seconds
h	hour

Variables (ECA droplets)

CMD	Count mean diameter (μm)
m_b	Mass of ECA yield bolus (mg)
V_b	Volume of ECA yield bolus (mL)
Φ_b	Flow of ECA yield bolus (mL/s)
V_T	Exhalation Tidal volume (mL)
t_p	Puff time (s)
N_p	Number of particles
d_p	Diameter of particles (μm or nm)
n_p	Particle number density (number per cm^3)
ρ_p	Particle mass density (grams per cm^3)
v_p	Particle velocity (cm/s)
Re_p	Particles Reynolds number (dimensionless)
t_{rel}	Particles relaxation time (s)
C_c	Cunningham slip factor (dimensionless)
λ	Mean molecular free path of air (μm)
U	Fluid (air) velocity (cm/s)
St	Stokes number (dimensionless)
t_f	Characteristic fluid (air) time (s)

Q	Airflow volume (cm^3/s)
V	Fluid (air) volume (cm^3)
T	Fluid (air) temperature ($^\circ\text{C}$)
ΔP	Pressure gradient ($\text{gm cm}^{-2}\text{s}^{-2}$)
Re_f	Fluid Reynolds number (dimensionless)
U_0	Exhalation velocity (cm/s)
t_{exh}	Exhalation time (s)

Variables (Respiratory particles: droplets and nuclei)

d_r	Diameter (μm or nm)
N_r	Numbers
n_r	Number density (numbers per cm^3)

Variables (Vaping jet/puff system)

d_0	Orifice diameter (cm)
ρ_a	air mass density (gm/cm^3)
μ	air dynamical viscosity ($\text{gm cm}^2/\text{s}$)
$[U_z, U_r, U_\phi]$	Components of jet velocity in cylindrical coordinates (cm/s)
U_{jc}	Centerline jet velocity (cm/s)
U_{pc}	Centerline puff velocity (cm/s)
U_e	Entrainment jet velocity (cm/s)
Q	Linear specific momentum of jet (gm cm/s)
Q_0	Linear specific momentum of jet at the orifice (gm cm/s)
\dot{Q}	Linear specific force of jet (gm cm/s^2)
\dot{Q}_0	Linear specific force of jet at the orifice (gm cm/s^2)
V_{pen}	Penetration volume (cm^3)
z_{jc}	Horizontal jet displacement (cm)
z_{j0}	Horizontal jet displacement at the orifice (cm)
z_{pc}	Horizontal puff displacement (cm)
z_{pd}	Virtual origin of puff displacement (cm)
t_{pd}	Time at virtual origin of puff displacement (s)

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Riccardo Polosa is full tenured professor of Internal Medicine at the University of Catania (Italy) and Medical Director of the Institute for Internal Medicine and Clinical Immunology at the same university. In relation to his recent work in the area of respiratory diseases, clinical immunology and tobacco control, RP has received lecture fees and research funding from Pfizer, GlaxoSmithKline, CV Therapeutics, NeuroSearch A/S, Sandoz, MSD, Boehringer Ingelheim, Novartis, Duska Therapeutics and Forest Laboratories. Lecture

fees from a number of European EC industry and trade associations (including FIVAPE in France and FIESEL in Italy) were directly donated to vaper advocacy non-profit organizations. RP has also received grants from European Commission initiatives (U-BIOPRED and AIRPROM) and from the Integral Rheumatology & Immunology Specialists Network (IRIS) initiative. He has also served as a consultant for Pfizer, Global Health Alliance for treatment of tobacco dependence, CV Therapeutics, Boehringer Ingelheim, Novartis, Duska Therapeutics, ECITA (Electronic Cigarette Industry Trade Association, in the UK), Arbi Group Srl. and Health Diplomats. RP has served on the Medical and Scientific Advisory Board of Cordex Pharma, Inc., CV Therapeutics, Duska Therapeutics Inc, Pfizer and PharmaCielo. RP is also founder of the Center for Tobacco prevention and treatment (CPCT) at the University of Catania and of the Center of Excellence for the acceleration of Harm Reduction (CoEHAR) at the same university, which has received support from the Foundation for a Smoke Free World to conduct eight independent investigator-initiated research projects on harm reduction. RP is also currently involved in the following pro bono activities: scientific advisor for LIAF, Lega Italiana Anti Fumo (Italian acronym for Italian Anti-Smoking League), the Consumer Advocates for Smoke-free Alternatives (CASAA) and the International Network of Nicotine Consumers Organizations (INNCO). RP is the Chair of the European Technical Committee for standardization on "Requirements and test methods for emissions of electronic cigarettes" (CEN/TC 437; WG4).