

## Article

# Design and Analysis of Slotted Waveguide Antenna Radiating in a “Plasma-Shaped” Cavity of an ECR Ion Source

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**Abstract:** The design of a microwave antenna sustaining a high-energy-content plasma in Electron Cyclotron Resonance Ion Sources (ECRISs) is, under many aspects, similar to the design of a conventional antenna but presenting also peculiarities because of the antenna lying in a cavity filled by an anisotropic plasma. The plasma chamber and microwave injection system design plays a critical role in the development of future ECRISs. In this paper, we present the numerical study of an unconventionally shaped plasma cavity, in which its geometry is inspired by the typical star-shaped ECR plasma, determined by the electrons trajectories as they move under the influence of the plasma-confining magnetic field. The cavity has been designed by using CST Studio Suite with the aim to maximize the on-axis electric field, thus increasing the wave-to-plasma absorption. As a second step, an innovative microwave injection system based on side-coupled slotted waveguides is presented. This new launching scheme allows an uniform power distribution inside the plasma cavity which could lead to an increase of ion source performances in terms of charge states and extracted currents when compared to the conventional axial microwave launch scheme. Finally, the use of both the “plasma-shaped” cavity and the microwave side coupled scheme could make the overall setup more compact.

**Keywords:** slotted waveguide antenna; waveguide coupler; wave-plasma coupling; resonant cavity; Electron Cyclotron Resonance Ion Sources (ECRIS)



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## 1. Introduction and Motivation

The coupling of microwaves into a plasma-filled cavity through one or more injection waveguides is a fundamental aspect in Electron Cyclotron Resonance Ion Sources (ECRISs). The source performances in terms of charge states and extracted currents has been explained by taking into account the different patterns of the electromagnetic field that is excited into the cavity, for a specific frequency (or set of frequencies) [1,2]. In order to enhance the source performances, several approaches have been used in the past years, such as the modification of the plasma cavity trying to better match the confining magnetic field profile [3], and the improvement of the microwave injection system by using modified or better cavity-matched waveguide configurations [4–7].

In this work, we compare the performances of different antenna systems radiating into cavities, possessing conventional and unconventional shapes, that can be modeled as a reverberation chamber. We discuss the possible antenna configurations and we present the numerical design of a novel plasma cavity in which its shape has been determined by the electron trajectories as they move under the influence of a *minimum-B* magnetic field profile (i.e., a typical configuration used in ECRISs). The modal configuration introduced into the presented cavity is compared with that of a standard cylindrical cavity, for the same frequency interval. It will be shown that the new cavity’s shape promotes the excitation

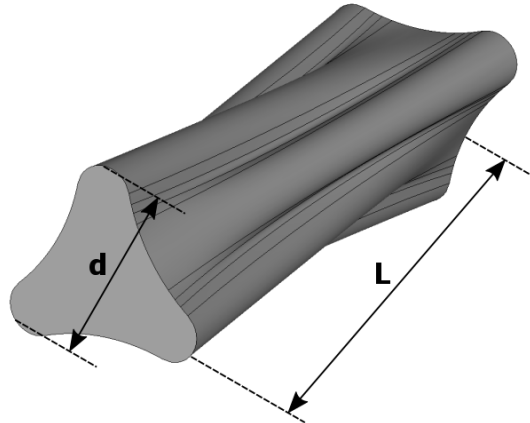
of modes with an electric field maximum along its axis, where the plasma is typically generated. This could be advantageous in terms of plasma absorbed power, preventing the formation of the typical hollow plasma experimentally observed when the excited mode has an electric field minimum along the cavity's axis [8]. In fact, for a circular cylinder shaped cavity, TE and TM modes are expressed in terms of Bessel functions (and first derivative of Bessel functions), all equal to zero at the origin except the  $J_0$  ( $J_1'$ ) [9].

As a second step, aiming at improving the ion source performances, we present a radically innovative microwave launching scheme that employs slotted waveguides which are side-coupled to the plasma cavity. It will be shown that this technique greatly improves the number of modes coupled inside the cavity with respect to the standard axially-coupled rectangular waveguide and at the same time makes possible a more homogeneous power transfer to the plasma thanks to the slots placed along the cavity outer wall. In addition, more space for other ancillaries is made available on the cavity's injection flange.

Due to the non-conventional shape of the novel "plasma-shaped" cavity and relative twisted slotted waveguide injection system, standard manufacturing techniques based on subtractive processes could be difficult to employ. To overcome these difficulties, for the future realization we plan to use additive manufacturing techniques, and in particular 3D metal printing through high quality metal powder compound.

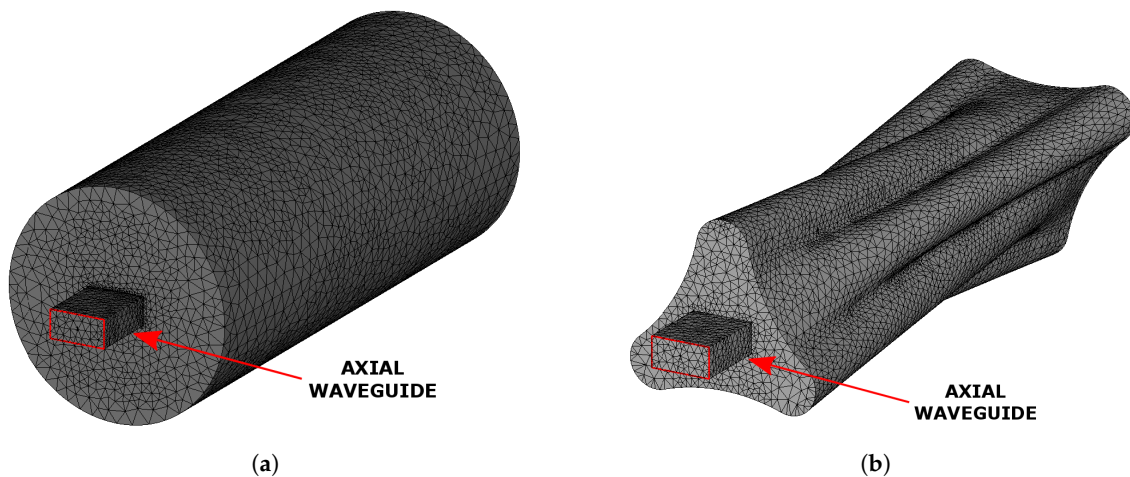
## 2. Plasma Shaped Cavity and Axial Microwave Injection

In Figure 1, the "plasma-shaped" cavity is shown with its main dimensions. The cavity has diameter  $d = 48.5$  mm and length  $L = 150$  mm, which are typical dimensions for a second generation ECRIS plasma chamber [10]. As said, the cavity's shape has been obtained by taking into account the electron trajectories as they move under the influence of a *minimum-B* magnetic field profile which is used for the plasma confinement in ECRISs [11].



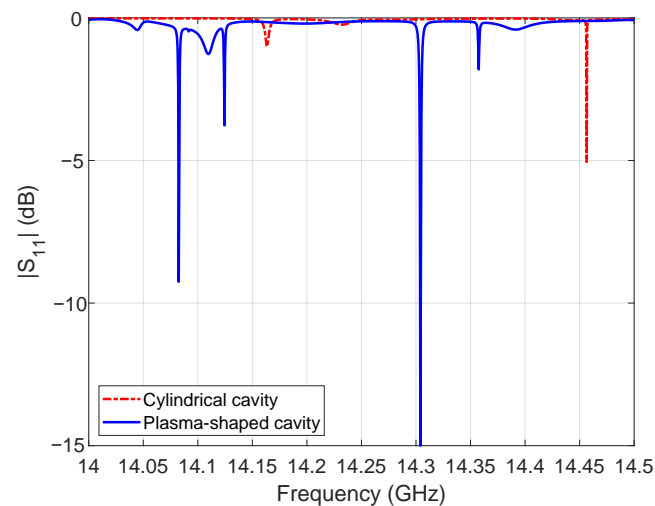
**Figure 1.** "Plasma-shaped" cavity with its main dimensions: diameter  $d$  and length  $L$ .

As first step of this numerical study, we compare the "plasma-shaped" S-parameters (i. e., the number of modes excited inside the cavity) with those of a standard cylindrical cavity usually employed in ECRISs setups. The adopted cylindrical cavity has a diameter  $d = 63.5$  mm and a length  $L = 150$  mm: these dimensions, comparable with those adopted for the "plasma-shaped" cavity, are the dimensions of the CAESAR Ion Source plasma cavity currently working at the INFN-LNS. Both cavities, initially fed through a standard WR62 axial waveguide, have been simulated with comparable settings: both consist of a vacuum solid with lossy metal boundary conditions and with the same mesh quality (e.g., curvature tolerance, number of mesh refinement steps). For both cavities, we consider finite conductivity walls with  $\sigma = 5.8 \times 10^7$  S/m. The two geometries with the applied mesh are visible in Figure 2.



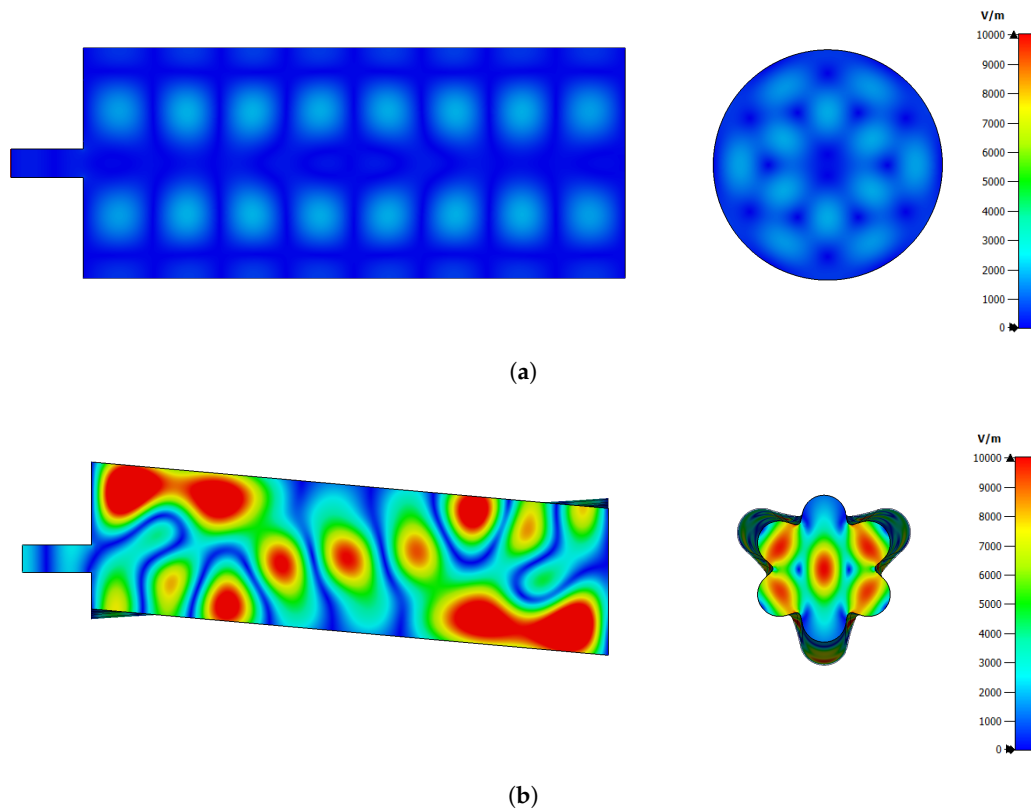
**Figure 2.** (a) Standard cylindrical cavity and (b) “plasma-shaped” cavity models. Applied mesh and axial feeding waveguides are visible.

The two structures have been analyzed in terms of S-parameters. In particular, the  $|S_{11}|$  has been evaluated in the frequency range of 14–14.5 GHz. The frequency interval has been selected in order to employ the future “plasma-shaped” cavity with the CAESAR ion source setup. The  $|S_{11}|$  curve for the two geometries is shown in Figure 3. In the case of cylindrical plasma cavity, very few and bad adapted modes are found inside the chosen frequency range (i.e., not optimal power transfer from the feeding waveguide to the cavity), while, in the case of the “plasma-shaped” cavity, more modes can be found in the same frequency range. In particular, the mode found at the frequency of 14.304 GHz presents a good waveguide-to-cavity coupling ( $|S_{11}| \simeq -15$  dB) and the related electric field profile has a maximum around the cavity center, where the plasma usually forms, as seen in Figure 4.



**Figure 3.**  $|S_{11}|$  curve, inside the operational bandwidth of 14–14.5 GHz, for the standard cylindrical cavity and the “plasma-shaped” one.

The above configurations, with the same mesh quality, can be simulated in around 20 and 30 min, respectively, with CST Studio Suite on a workstation i7 with 28 cores and 192 GB of ram.



**Figure 4.** Electric field module plot on side and front slices for: (a) cylindrical cavity ( $f_0 = 14.457$  GHz) and (b) “plasma-shaped” cavity ( $f_0 = 14.304$  GHz). Electric field has been normalized to the maximum value of 10 kV/m.

### 3. Slotted Waveguide Antenna Design

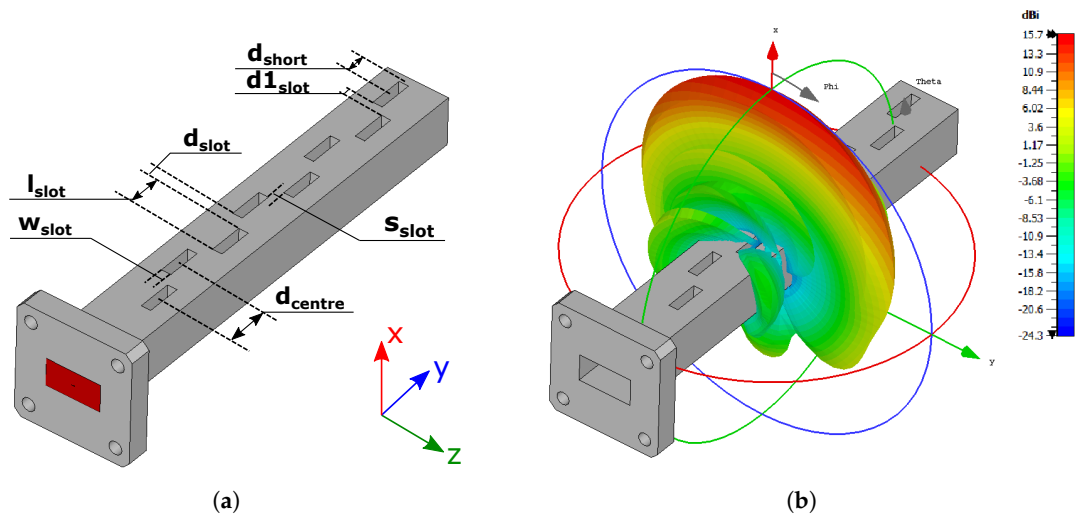
With the aim to improve the microwave-to-cavity coupling and at the same time to have a more uniform and symmetric axial electric field distribution, a radically new microwave injection system has been employed. A slotted waveguide antenna operating in free space has firstly been studied, to explore its behavior as a function of the fundamental project parameters. A first preliminary antenna design is described in Reference [12]. Slotted waveguide antennas find many applications in radar and communication systems due to their low-profile design requirements, mechanical robustness, good efficiency, relative ease of realization and wide operational frequency bandwidth [13–15]. The guided wavelength for the  $TE_{10}$  mode of the rectangular waveguide is given as  $\lambda_g = \frac{c}{f \sqrt{1 - c/(2af)}}$ , where  $f$  is the operational frequency and  $a$  is the waveguide large side. The guidelines for the design of a slotted waveguide antenna can be easily found in literature [16,17]. The main design parameters of the simulated slotted waveguide antenna are listed in Table 1. Among these, some critical ones can be highlighted, particularly the width and length of the slots,  $w_{slot}$  and  $l_{slot}$ , respectively, and the distance between the last slot center and the closing short wall or  $d_{short}$ . The number of employed slots is also a critical parameter that needs to be taken into account during the antenna project. In fact, the impedance bandwidth is inversely proportional to the slot number. On the contrary, the antenna efficiency increases with the slot number. In general, a trade-off for this parameters is chosen depending on the required performances. The slotted waveguide antenna, shown in Figure 5, has been optimized through the use of CST Studio Suite. The operational bandwidth is 14.2–15.25 GHz with central frequency 14.7 GHz. Eight slots have been employed in order to maximize the  $|S_{11}|$  impedance bandwidth and at the same time to preserve the radiation efficiency (near 100% in the numerical simulations). The slot number has also been chosen considering the available space along the cavity outer wall, equal to 150 mm. A tuning of the previously reported critical parameters ( $w_{slot}$ ,  $l_{slot}$ ,  $d_{short}$ ) has been

performed through a cycle of parametric steps in order to observe their effect on the antenna impedance bandwidth [18]. The calculated  $|S_{11}|$  curves are shown in Figure 6. After an optimization phase, a good compromise between impedance bandwidth and efficiency has been found by setting  $w_{slot} = 1.75$  mm,  $l_{slot} = 9.92$  mm and  $d_{short} = 6.455$  mm.

It is worth to point out that, when the ECRIS is operated at a frequency  $< 18$  GHz, a wide operational bandwidth is desirable in order to employ the frequency tuning effect to boost the source performances in terms of charge states and extracted currents [19]. When the slot number is increased, the antenna directivity increases at the cost of a narrow operational bandwidth: such a characteristic could be an advantage exploitable in the future generation of ECRIS operating at higher frequencies and powered through narrow bandwidth amplifiers.

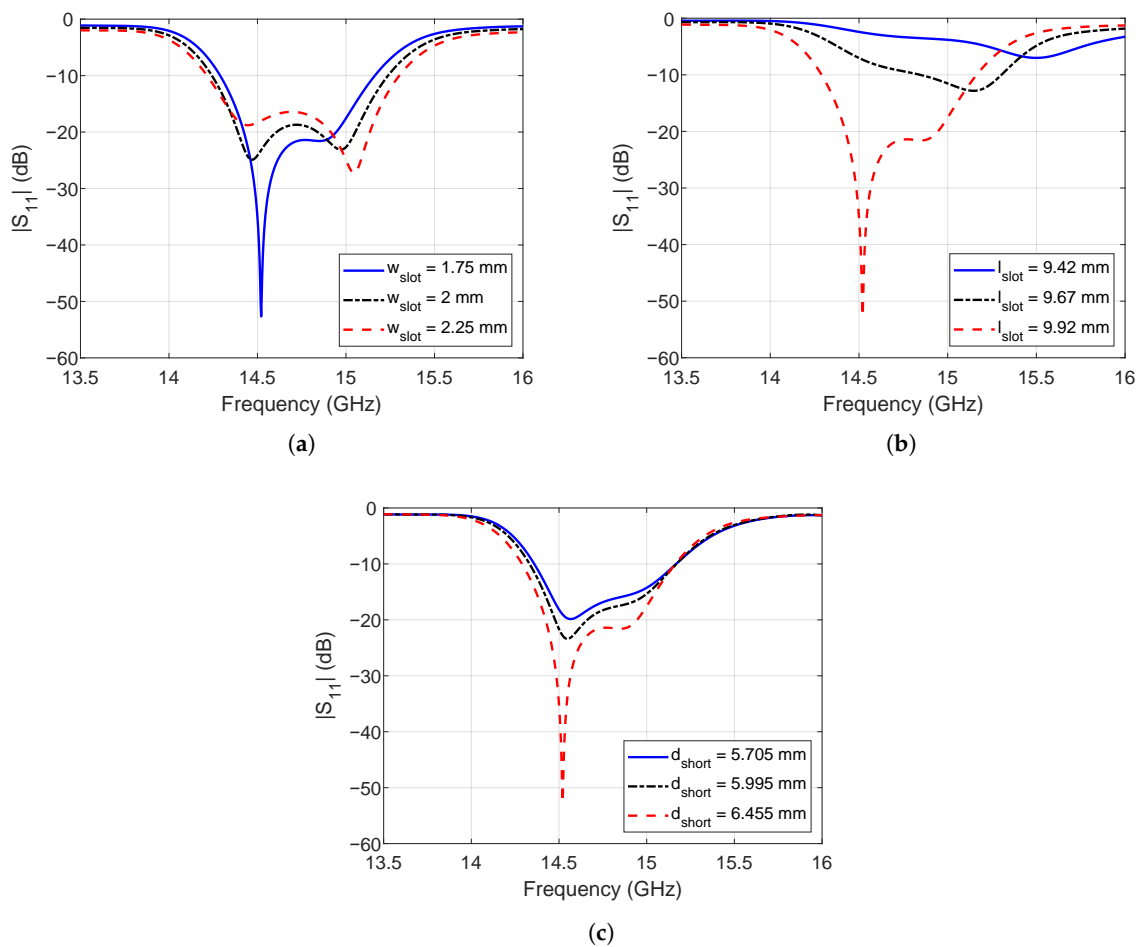
**Table 1.** Slotted waveguide antenna main design parameters.

Parameter	Value [mm]	Description
$l_{slot}$	9.92	Slot length
$w_{slot}$	1.75	Slot width
$d_{center}$	13.45	Slot centers distances
$d_{slot}$	3.53	Longitudinal distance between slots
$d1_{slot}$	2.53	Last two slots distance
$s_{slot}$	2.75	Transversal distance between slots
$d_{short}$	6.455	Last slot center to short wall distance

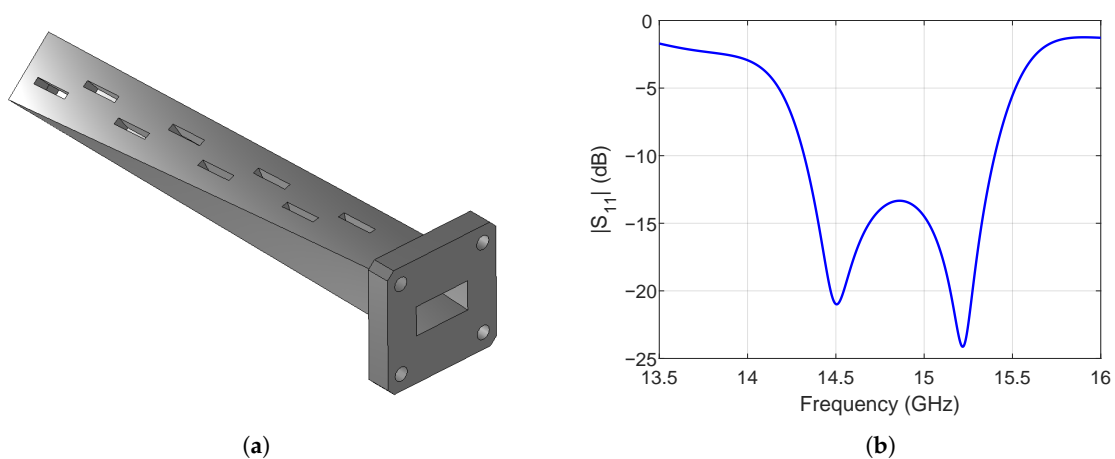


**Figure 5.** (a) Slotted waveguide antenna model with fundamental design parameters highlighted. The structure consists of a steel block (grey object) fed through a waveguide port, highlighted in red. (b) Farfield pattern of the presented slotted waveguide antenna.

As a final step, in order to employ the slotted waveguide as microwave launcher for the “plasma-shaped” chamber, a twisted version of the antenna has been created and simulated. The slotted-twisted waveguide antenna is visible in Figure 7a: starting from the WR62 attach flange, a 45-deg twist has been applied to the waveguide body. The structure retains the same project parameters listed in Table 1, except from  $d_{short}$ , in which value has been set to 7.954 mm for optimization reasons. The  $|S_{11}|$  has been computed and is plotted in Figure 7b, showing that the antenna keeps good performances even with the applied twist.



**Figure 6.**  $|S_{11}|$  versus (a)  $w_{slot}$ , (b)  $l_{slot}$  and (c)  $d_{short}$ . For each parameter variation, the remaining ones have been fixed to the nominal design values reported in Table 1.

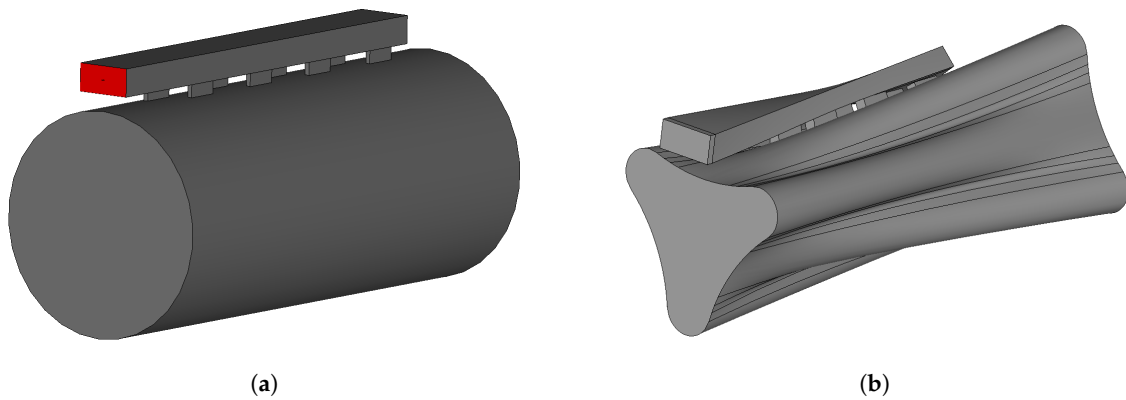


**Figure 7.** (a) Slotted-twisted waveguide antenna and (b) computed  $|S_{11}|$ . The antenna retains the design values reported in Table 1 except for  $d_{short}$ , now equal to 7.954 mm.

#### 4. Slotted Waveguide Injection Simulations

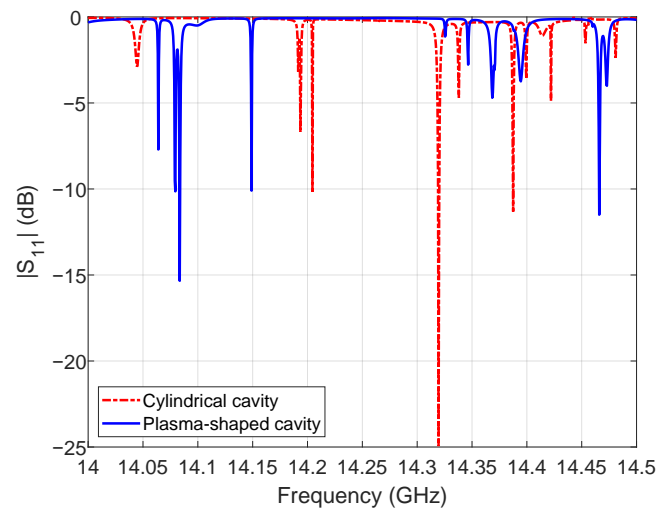
The previously studied slotted waveguides have been attached to the two plasma cavities in order to obtain the new microwave launch geometry. In the case of the “plasma-

shaped" cavity, the slotted waveguide has also been twisted in order to follow the outer wall shape. The two geometries (vacuum volumes) are visible in Figure 8.



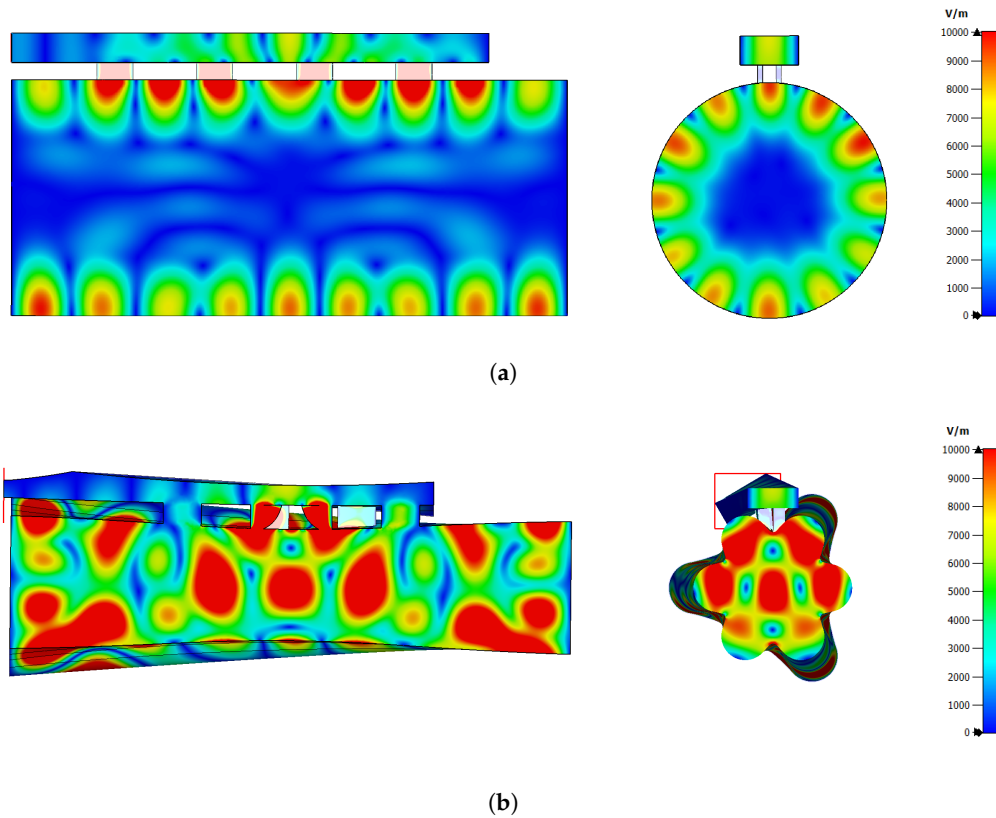
**Figure 8.** Slotted waveguide injection system coupled to: (a) standard cylindrical and (b) "plasma-shaped" cavities. Simulations have been made by using vacuum volumes.

The  $|S_{11}|$  curves have been calculated for both cavities with the new slotted waveguide microwave injection system, as shown in Figure 9. From the plot it can be observed that, using the new microwave injection system, more modes are coupled inside both cavities with respect to the standard axial one. This could be advantageous when one applies the frequency tuning technique in order to improve the ion source performances.



**Figure 9.**  $|S_{11}|$  curve, for the standard cylindrical cavity and the "plasma-shaped" one with the slotted waveguide microwave injection system, inside the operational bandwidth of 14–14.5 GHz.

The electric field plot, at the frequency of 14.466 GHz, inside the "plasma-shaped" cavity employing the side-coupled slotted waveguide is shown in Figure 10b. It can be seen that the field presents a maximum around the cavity center and its profile results now symmetric along the cavity axis with respect to the configuration shown in Figure 4 relative of the axial injection system. It is worth noting that, with the same side-coupled slotted waveguide, the cylindrical cavity still presents a predominance of modes with off-axis electric field maxima, as seen in Figure 10a.



**Figure 10.** Electric field module plot on side and front slices for: (a) cylindrical cavity ( $f_0 = 14.388$  GHz) and (b) “plasma-shaped” cavity ( $f_0 = 14.466$  GHz) employing the side-coupled slotted waveguide injection system. Electric field has been normalized to the maximum value of 10 kV/m.

The obtained field symmetry leads to a homogeneous power distribution inside the cavity from the multiple radiating slots, with a potential advantage in terms of power absorbed from the plasma. Furthermore, the use of the slotted waveguide could in principle lead to an increase of the total employable power by creating a splitted-injection system composed of multiple slotted waveguides placed radially with respect to the cavity [20].

## 5. Conclusions and Perspectives

In this work, injection schemes for plasma cavity of ECR ion sources were studied and compared, considering both conventional and innovative plasma chambers. In particular, an advanced antenna for the new chamber shape is studied. This new and groundbreaking antenna and cavity system is twisted so that the cavity volume resembles the electrons trajectories as they move under the influence of the confining magnetic field. The employed shape presents some advantages with respect to a classical cylindrical cavity usually employed in ion source setups. In particular, modes having an electric field profile with maximum near the cavity center, where the plasma usually generates, can be excited. Moreover, the electron-shaped geometry occupies less radial volume, providing more space for the magnetic system axial coils, which turns out to be advantageous for a fine tuning of the plasma-confining magnetic field. Such non-conventional cavity can be coupled to a radically innovative microwave injection. In view of this, a system based on a side-coupled slotted waveguide has been conceived and studied. The slotted waveguide has firstly been analyzed as an antenna operating in free space in order to test its behavior versus the fundamental tuning parameters. Subsequently, the slotted waveguide has been jointed to the two plasma cavity geometries and the two structures behavior has been studied in terms of S-parameters. Numerical results show that the new injection system greatly improves the excited modes inside the frequency band of interest, which could be useful in ion source frequency tuning operations. From the simulation, it has also been



found that the use of the “plasma-shaped” cavity in conjunction with the slotted waveguide injection system results in an axially-symmetric field distribution of the excited modes, and this could allow a more uniform power transfer to the plasma from the radiating slots. Furthermore, the use of the side-coupled slotted waveguide also allows more space on the cavity injection flange, employable for other ancillaries.

The plasma-load effect will be predicted by our full-wave numerical tool considering the self-consistent interplay between the microwave field and a fully anisotropic 3D plasma filling the cavity [21,22]. Ongoing simulations already show higher robustness of modal structures established in this kind of cavities.

Finally, experimental characterization of the future slotted waveguide and plasma-shaped cavity prototypes will be performed, in terms of S-parameters and electric field measurements, in order to quantify the performance impact of internal surface roughness derived from the additive manufacturing versus standard realization technique. Preliminary vacuum tests on a pair of 3D metal printed containers samples have already been performed with positive and promising results.

**Author Contributions:** G.T. and D.M. addressed the conceptualization of the “plasma-shaped” cavity. G.T., O.L., G.S., G.S.M. and D.M. are responsible for the methodology of the study, including analysis and development of the cavity and slotted waveguide microwave injection system. G.S.M., G.T. and O.L. carried out the cavity, antenna and final assembly numerical simulations and optimization. Writing-original draft preparation, G.S.M.; writing-review and editing, G.S.M., G.T., G.S., A.P. and D.M.; supervision and project administration, D.M. All authors have read and agreed to the published version of the manuscript.

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**Conflicts of Interest:** The authors declare no conflict of interest.

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